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# Numerical study to understand thermo-mechanical effects on a composite-aluminium hybrid bolted joint

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## Abstract

Hybrid bolted joints, where carbon fiber reinforced polymers and metallic plates are clamped using bolts, are widely used in aircraft structures. During operation, aircraft experience extreme temperatures that can adversely affect the response of an hybrid joint. On account of the lack of understanding on this aspect, we analyzed a representative carbon-aluminum single lap shear bolted joint using a 3D numerical model. A parametric study varying the temperature, friction coefficient, bolt clamping force, bolt-hole clearance, and thickness of the metallic plate, provided insight into their effect on the stiffness stages of the mechanical response of the joint, as well as the contact evolution among the different elements. Bolt-hole clearance was one of the parameters that most influenced the joint stiffness and bolt bending. Temperature excursions induced sliding between plates and significantly altered the clamping load of the bolt, i.e., a 40% reduction and an 18% increase for a negative and positive thermal jumps, respectively. This clamping load variation entails undesirable bolt loosening or even yielding. Therefore, this work sheds light on the detrimental effects of temperature on hybrid joints, thus providing background for a safer structural design.

*Keywords:* Hybrid bolted joints, Thermal effect, Aircraft structure, Joint response

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## 1. Introduction

Bolted joints are extensively used in aeronautical structures due to their efficiency in transferring load and ease of service and repair[1; 2]. Understanding the mechanical response of a bolted joint is complex because of the contact interaction of several parts and the stress concentrations at the bolt hole. Despite the considerable amount of published work [3; 4], the design of bolted joints is still a challenging task, particularly when environmental factors need to be accounted for.

In the last decades, aircraft industries have increased the use of Carbon Fiber Reinforced Polymer (CFRP) materials, but at the same time have maintained metallic components (aluminium, titanium) in the primary structure of the aircraft. This has led to hybrid joint assemblies routinely found in structural components such as the wings, empennage or fuselage. For example, the Airbus A380 utilizes lightweight carbon fiber skins connected to aluminium ribs in its wings. However, within a

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31 few years of service, cracks have been found on the rib feet which had originated from the rib-to-skin  
32 panel attachment holes. In addition, cracks were found at the vertical web of the rib feet [5]. The  
33 Airworthiness Directive issued by the FAA, stated that this condition could potentially affect the  
34 structural integrity of the aircraft. Preliminary investigations accounted this to the high stresses at  
35 the joint between dissimilar materials and also to differential response to extreme temperatures [6].  
36 This critical situation evidences that there is still a need to adequately understand the response of  
37 hybrid bolted joints under different operating conditions.

38 An aircraft experiences temperatures in the range of  $-30^{\circ}\text{C}$  to  $-55^{\circ}\text{C}$  at cruising altitudes, and  
39 between  $45^{\circ}\text{C}$  to  $50^{\circ}\text{C}$  when landed, depending on the destination airport. The difference in the thermal  
40 expansion coefficient of carbon and aluminum induces differential expansion/contraction, leading to  
41 difficult-to-predict thermal stresses and uneven responses in the bolted plates, as well as significant  
42 variations in the bolt clamping forces. Studies on the thermal load effects on dissimilar material  
43 bolted joints are barely touched on the literature [7]. That said, Coman et al. [7] experimentally and  
44 numerically studied the temperature effect damage initiation and propagation have on a hybrid bolted  
45 joint using strain gauge measurements and a 3D finite element model with damage. Other researchers  
46 [8–10] concentrated on the dependence of the bearing strength and damage modes of bolted joints at  
47 different temperatures. However, a lack of understanding still remains as to how thermal loads affect  
48 the bolts' preload, the sliding of the dissimilar parts and the evolution of the contact forces between  
49 the different parts.

50 Apart from the thermal effects, there are several joint parameters that affect a bolted joint's  
51 response [11; 12]. McCarthy et al. [13; 14] experimentally investigated the effect bolt-hole clearance  
52 has on the composite-composite bolted joint strength and stiffness and reported a 10% joint stiffness  
53 loss due to an increase in the bolt-hole clearance; contrary to the findings reported in [15]. The same  
54 authors [16; 17] also numerically studied the bolt-hole clearance effect using 3D finite element analysis  
55 and concluded this parameter is crucial in the design of bolted joints. Friction is another important  
56 parameter and the least discussed in the literature. The coefficient of friction value varies depending on  
57 the material of the joining parts, surface treatment, surface ply orientations in a composite laminate,  
58 etc., [18; 19]; all of which potentially affect the response of the joint. The friction coefficient is quite  
59 complex to determine experimentally [20]. Regarding the bolt preload, Oskouei et al. [21] studied the  
60 variation in the preload clamping force due to applied longitudinal tensile load applied in an aerospace  
61 bolted plate. Lv et al. [22] concluded that there was a significant change in the bolt preload when the  
62 temperature and the initial preload were varied.

63 In addition to the experimental tests [23], researchers have used analytical [24–26] and numerical  
64 methods [4; 9; 27–33] to predict the behavior of bolted joints. While the former is efficient in the  
65 preliminary design stage, the latter is required for detailed understanding and accurate predictions. In

66 the framework of Finite Element (FE) analysis, early researchers used simplified models to economically  
67 study bolted joints. Kim et al. [34] investigated different bolt modeling cases such as using 3D solid  
68 or beam elements and also compared the results with a no bolt case (where a pretension was directly  
69 applied to the washer surface without physically modeling a bolt). They concluded that for accurate  
70 responses, it is important to use 3D models that take into account the contact interactions, bolt preload  
71 and complex 3D stress states around the bolts. Advances in FE tools have made it possible to virtually  
72 study the effect of several parameters on the response, which is quite infeasible experimentally.

73 This work is set within the framework of an ongoing EU Cleansky 2 project ‘INNOHYBOX’,  
74 developed by the consortium of Dassault Aviation, University of Girona, Eurecat and Sofitec. The  
75 global objective of the project is to experimentally and numerically analyze the hybrid wing box  
76 of an aircraft under thermo-mechanical loads. The study presented here is a primary investigation  
77 performed at a coupon level to understand the bolted joint response. Using a detailed 3D numerical  
78 model, we study the thermo-mechanical response of a single lap shear bolted CFRP-aluminium joint  
79 with a countersunk fastener by simulating bolt preload, thermal step and followed by a static tensile  
80 test. The different stages of the joint response and the evolution of the contact surfaces are discussed,  
81 and the contribution of the frictional and normal forces at each stage presented. Further, we perform  
82 an exhaustive parametric study to study what the effects of friction coefficient, bolt clamping force,  
83 bolt-hole clearance and the thickness of the aluminium plates have. More importantly, we simulate  
84 a temperature jump (positive or negative) before the tensile loading and demonstrate the significant  
85 effect this has on the bolt clamping load and contact evolution. Finally, to reproduce the conditions  
86 of aircraft in service, we simulated a loading-unloading-reloading loop.

## 87 **2. Methodology**

### 88 *2.1. Numerical model*

89 We developed a detailed 3D numerical model of a Single Lap Shear (SLS) bolted joint in ABAQUS  
90 Standard 6.14 [35], using the implicit static solver framework. Fig. 1 illustrates the SLS specimen  
91 containing the following parts: i) a CFRP multi-directional laminate made of 60 plies leading to a  
92 total thickness of 7.8 mm; ii) an aluminium plate with a thickness of 6 mm; iii) a countersunk fastener  
93 made of steel with a shank diameter of 4.78 mm and a countersunk angle of  $100^\circ$  and iv) doubler  
94 (CFRP and aluminium) plates placed on either side of the specimen to counteract the moments in an  
95 SLS specimen. Table 1 details the different materials used and their corresponding material properties  
96 (taken from [36]).

97 Fig. 1 also depicts the dimensions of the SLS specimen, which are mostly in accordance with the  
98 ASTM standard D5961/D5961-M [37]. All the parts were modeled individually and assembled in the

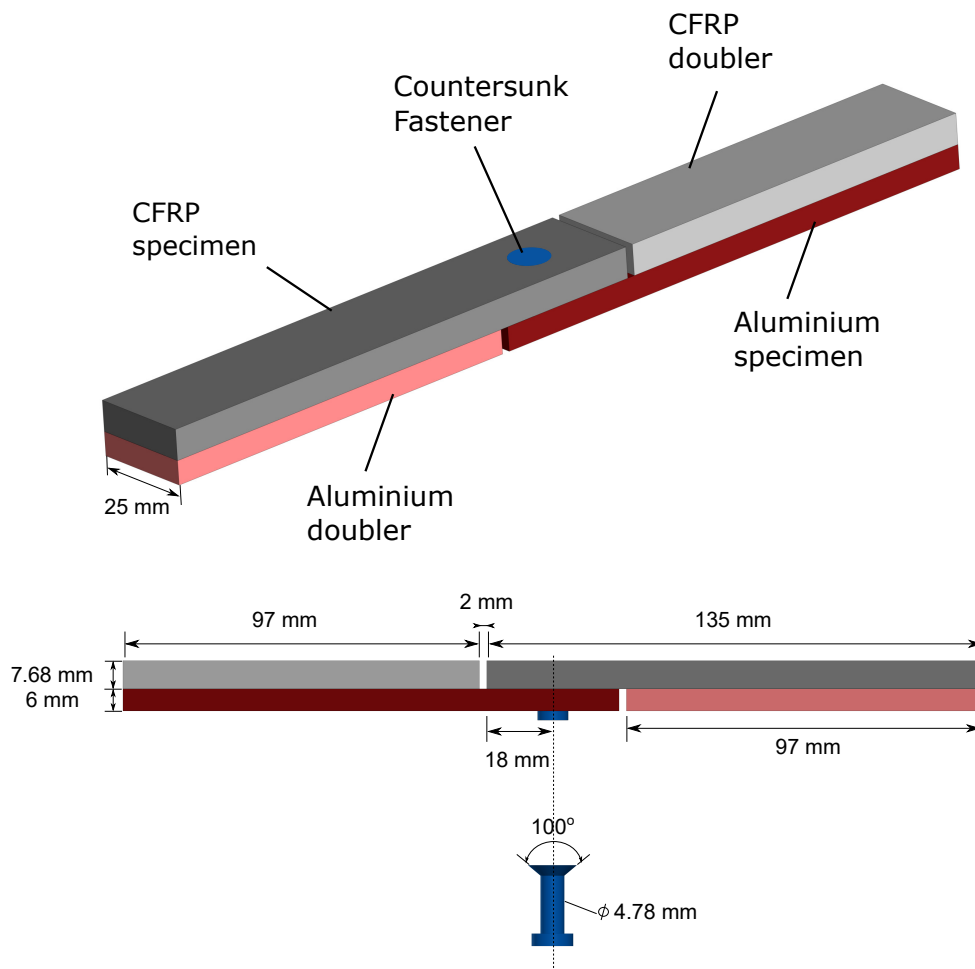


Figure 1: Schematic illustration of the single lap shear bolted joint comprising of CFRP-aluminium plates with a steel countersunk fastener, along with the dimensions of the different parts.

Table 1: Different materials used and the respective material properties (Taken from [36]).

Material	Property	Value
Steel alloy	$E$ [MPa]	21000
	$\nu$ [-]	0.3
	$\alpha$ [ $\mu\text{m}/\text{m}^\circ\text{C}$ ]	11
	$\rho$ [ $\text{g}/\text{cm}^3$ ]	8
Aluminium (Al 2024-O)	$E$ [MPa]	73100
	$\nu$ [-]	0.33
	$\alpha$ [ $\mu\text{m}/\text{m}^\circ\text{C}$ ]	21.1
	$\rho$ [ $\text{g}/\text{cm}^3$ ]	2.7
CFRP (M21 EV/ IMA)	$E_{11}$ [MPa]	165000
	$E_{22}$ & $E_{33}$ [MPa]	9300
	$\nu_{12}$ & $\nu_{13}$ [-]	0.35
	$\nu_{23}$ [-]	0.487
	$G_{12}$ & $G_{13}$ [MPa]	5080
	$G_{23}$ [MPa]	3127.1
	$\alpha_{11}$ [ $\mu\text{m}/\text{m}^\circ\text{C}$ ]	0.6
	$\alpha_{22}$ & $\alpha_{33}$ [ $\mu\text{m}/\text{m}^\circ\text{C}$ ]	33
	$\rho$ [ $\text{g}/\text{cm}^3$ ]	1.5
	Ply thickness [mm]	0.13

99 Abaqus Assembly module. Here the nut and bolt (without a washer) are modeled as a single part  
100 because the movement between the bolt and nut is considered not significant. The entire model is  
101 meshed using C3D8R elements; an 8 noded 3-dimensional brick element with reduced integration. A  
102 finer mesh was used at the vicinity of the plate-hole region and for the countersunk bolt (Fig. 3).

103 All the three materials (CFRP, aluminium and steel) are modeled as linear elastic, as the focus  
104 of this study is to understand the different stages of the bolted joint response before the initiation  
105 of damage. In addition, damage is mostly associated to bearing and is reported to happen at high  
106 applied displacements [3]. CFRP is modeled as an orthotropic elastic material (along with the thermal  
107 expansion coefficients in three directions) and the plies are defined using the ‘Composite Layup’ feature  
108 in Abaqus/Standard [35]. Since the study focuses only on linear elastic part, basic linear elastic material  
109 constitutive laws from Abaqus [35] are used for the simulations.

110 The contact interaction is assigned at three regions: (a) between the carbon and the aluminium  
111 plates; (b) between the bolt shaft and the hole of the plates and (c) between the bottom plate and the

112 nut (modeled along with the bolt). This is simulated using the surface-to-surface contact algorithm  
113 in Abaqus/Standard, as recommended in Abaqus documentation [35] for the current problem. This  
114 interaction accounts for the friction and sliding between the contact surfaces, in addition to a hard  
115 contact over-closure relation. The hard contact defines the contact pressure between the two surfaces as  
116 a function of the over-closure of these surfaces (also referred to as the interpenetration of the surfaces).  
117 A small sliding tracking approach is assigned such that even if the bodies undergo large motions, there  
118 will be relatively little sliding. In addition, Abaqus uses an extended version of Coulomb's friction  
119 model [35] which accounts for the friction at the contact surfaces. Finite clearances are included  
120 between the bolt and the plate hole.

121 We defined the whole simulation in three steps, namely:

- 122 (a) Bolt pre-tension. The first step consists of applying a pretension force to the bolt by employing  
123 the 'Bolt Load' feature in Abaqus/Standard [35]. The elements underlying the pretension section  
124 are adjusted by Abaqus to obtain the prescribed amount of clamping force in the bolt. Further,  
125 this adjustment of the element length can be fixed so that the preload is maintained in the  
126 subsequent steps and the bolt can act as a deformable part when other loads are encountered  
127 [35].
- 128 (b) Thermal. Once the bolt has been tightened, a thermal step is performed to simulate the change  
129 in the thermal conditions, ranging from a room temperature (25 °C) to high (90°C) or low  
130 temperatures (-55°C). This temperature variation can be performed using the 'Predetermined  
131 field' option in Abaqus, where the target temperature and a ramp amplitude are specified.
- 132 (c) Tensile. Longitudinal tensile displacement is applied to one side of the assembly to simulate the  
133 shear response of the joint. All the nodes at one edge of the assembly are selected and applied a  
134 displacement in the in plane direction, while constraining the displacement in the other directions  
135 in order to have a pure in-plane loading. At the same time, nodes on the other edge are fixed.

136 Figure 2 presents the boundary conditions and applied load for the preload and tensile step for the  
137 SLS joint. During the bolt preload step, both the ends of the joint are clamped completely. During  
138 the thermal step, the same boundary condition as in the case of preload step is used. For the tensile  
139 loading, displacement is applied to all the nodes at one edge, while the other edge is still clamped.  
140 The force is obtained by summing all the reaction forces from the clamped joint end nodes.

141 In the bolt pre-tension and thermal steps, one of the options is to constrain all the degrees of freedom  
142 at one edge and leave the other free. This, however, lead to unfavorable out-of-plane movements.  
143 Hence, both ends of the assembly are constrained in all the degrees of freedom to simulate the bolt

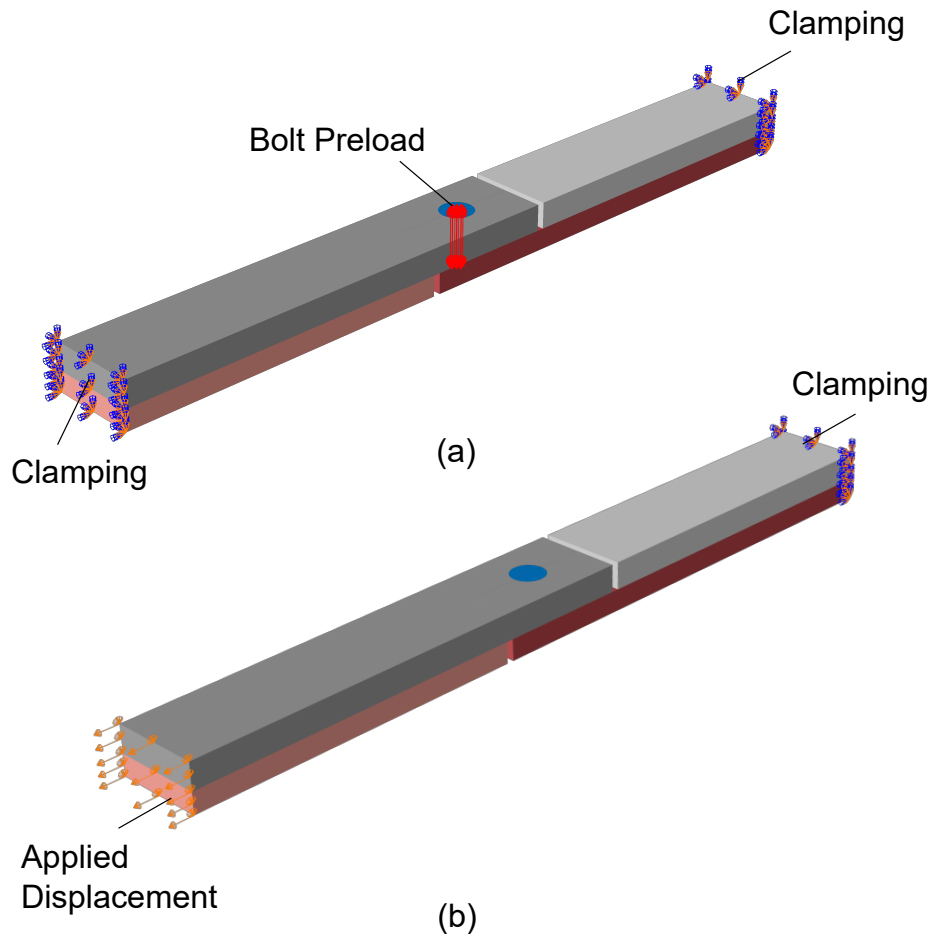


Figure 2: Load and boundary conditions detailed for (a) bolt preload and (b) tensile step.



144 preload and the temperature variation. In the tensile step, longitudinal displacement is applied to one  
145 side of the assembly, while the other end is constrained.

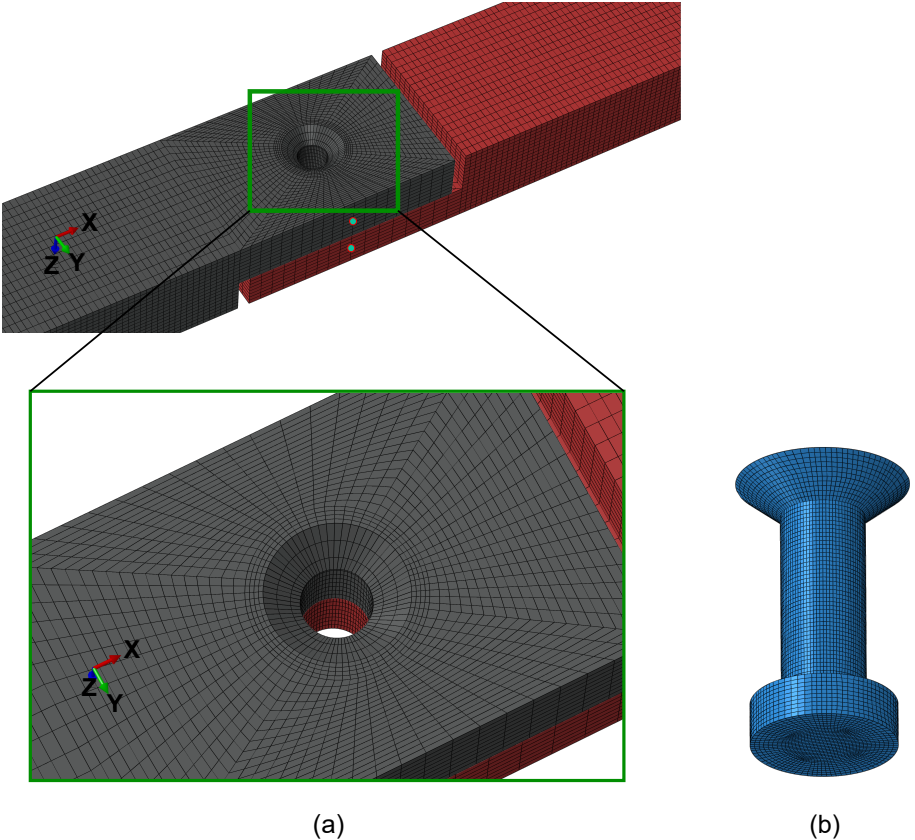


Figure 3: Details of the mesh discretization at the (a) bolt-hole region of the composite aluminium overlap region and (b) the countersunk fastener. (The top image also illustrates the extensometer locations (circles filled in green) to virtually measure sliding between the plates)

146 *2.2. Definition of parametric study*

147 Table 2 defines the different parameters the parametric study considers to understand their effect  
148 on the joint response. Case A is taken as the baseline. Here, the parameters correspond to typical  
149 values from references: a friction coefficient of 0.3 is considered. The other values considered to study  
150 the influence of high and low friction on joint behavior are 0.6 and 0.15, respectively. A clamping force  
151 of 6000 N (equivalent to a torque of 3.4 Nm) is considered as the baseline (in accordance with ASTM  
152 standards [37]), whereas a ‘hand-tight’ torque of 0.5 Nm, equivalent to a clamping force of 750 N, is  
153 selected as the other value. The selected clamping forces also ensure that there is no yielding in the  
154 bolt under the applied torque.

155 Typical aerospace structures use a bolt-hole clearance (defined as the difference in the diameter  
 156 between hole and bolt shaft) in between 50-150  $\mu m$  ([13; 38]), and in this study the baseline is taken  
 157 as 60  $\mu m$ . In addition, a higher clearance of 200  $\mu m$  is explored to study the effects out-of-tolerance  
 158 cases have on the joint behavior. Further, the influence of varying the thickness of the aluminium  
 159 plate (a common industrial practice used to optimize the assembly depending on the loads) is also  
 160 studied. Apart from the baseline value of 6 mm, thinner (4 mm) and thicker (9 mm) aluminium plates  
 161 were investigated. As a final parameter and the main focus of this study, the thermal conditions were  
 162 varied from room temperature to a positive thermal jump of 65 ( $25^{\circ}C$  to  $90^{\circ}C$ ) or a negative one of  
 163 80 ( $25^{\circ}C$  to  $-55^{\circ}C$ ).

Table 2: Definition of the parameters for each case study

Case	Friction coefficient ( $\mu$ ) (-)	Bolt clamping force (CF) ( $N$ )	Bolt-hole clearance (BC) ( $\mu m$ )	Aluminium thickness ( $t_{Al}$ ) ( $mm$ )	Thermal gradient ( $\Delta T$ ) ( $^{\circ}C$ )
A (Baseline)	0.3	6000	60	6	0
B	0.15	6000	60	6	0
C	0.6	6000	60	6	0
D	0.15	750	60	6	0
E	0.3	750	60	6	0
F	0.3	6000	200	6	0
G	0.3	6000	60	4	0
H	0.3	6000	60	9	0
I	0.3	6000	60	6	-80
J	0.3	6000	60	6	+65

164 Table 3 summarizes how the comparison of several cases from Table 2 allows for the effect of each  
 165 investigated parameter on the joint response to be discussed.

Table 3: Compared cases and their corresponding targeted effects

Cases compared	Effect studied
A, B, C	Friction coefficient
A, E and B, D	Bolt clamping force
A, F	Bolt-hole clearance
A, G, H	Aluminium thickness
A, I	Negative thermal
A, J	Positive thermal

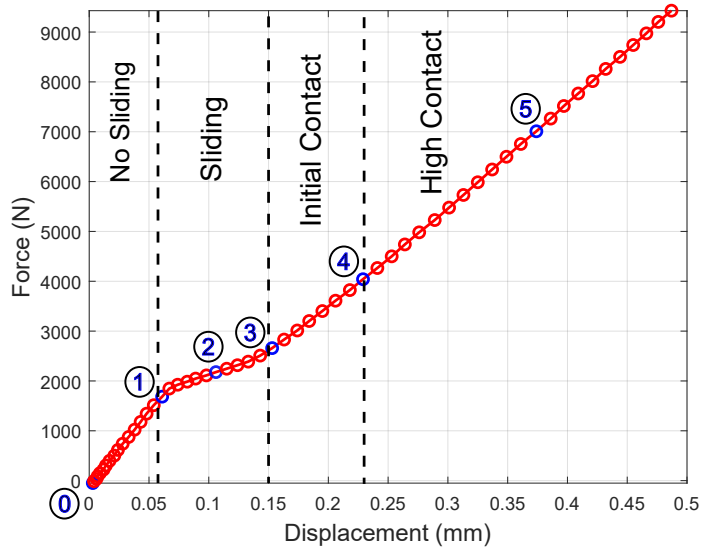
### 166 3. Results and Discussion

#### 167 3.1. Mechanical response of a bolted joint

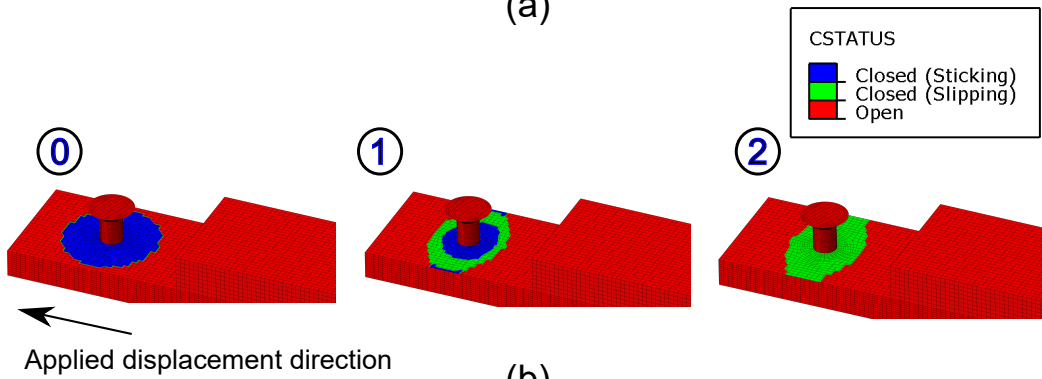
168 Fig. 4 (a) presents the force-displacement response of the baseline case under tensile loading. Here  
169 the plotted displacement is the one that is applied to all the nodes of the joint end and the force  
170 represents the reaction force obtained from the nodes at the other joint end that is clamped. The  
171 main objective is to understand the different stiffness stages in the shear response of the bolted joint.  
172 The same figure also illustrates the evolution in the contact status between the two plates (in Fig. 4  
173 (b)) and the bolt shaft region under contact with the plates (in Fig. 4 (c)). Contact status is studied  
174 using CSTATUS output provided by Abaqus [35], where we can identify if the surfaces are completely  
175 in contact or in contact but sliding or no longer in contact.

176 The joint response can be divided into different stiffness stages, namely Stage I (0-1), Stage II (1-3),  
177 and Stage III (3-5). Stage I records the highest stiffness out of all the stages and no sliding between  
178 the plates is recorded (as seen in Fig. 4 (b)). No relative movement between the plates signifies that  
179 the load is carried by friction, and the maximum load taken by friction is the product of the clamping  
180 force (6000 N) and the coefficient of friction (0.3), i.e., around 1800 N (as seen in 4 (a)). Stage II (1-3),  
181 characterized by the sliding of the plates, starts when the load transferred by friction is surpassed,  
182 and the stiffness of this stage is much lower than that of Stage I. The relative movement between the  
183 plates starts and the closed contact status created by the preload clamping force changes to sliding  
184 (Fig. 4 (b)). The sliding of the plates continues until the bolt shaft comes in contact with the hole  
185 of the plates, which marks the beginning of Stage III (3-5). Fig. 4 (c) represents the evolution in the  
186 area of contact between the bolt shaft and the plates. The stiffness of Stage III is lower than that of  
187 Stage I, and with increasing displacement applied, the contact area between the bolt shaft and the  
188 hole increases.

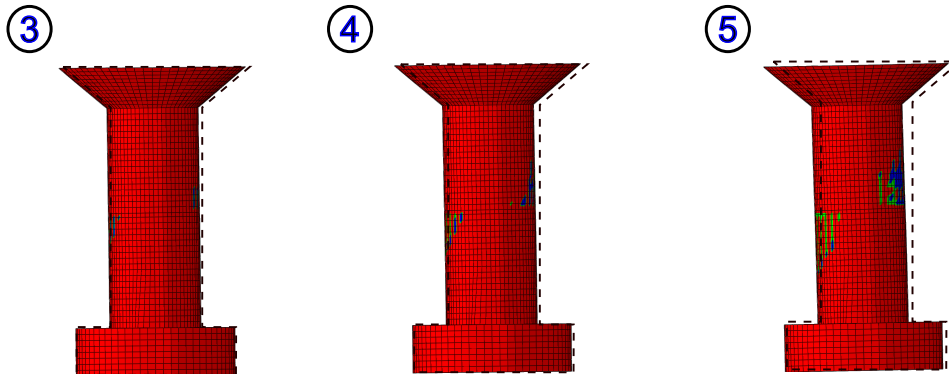
189 The 3D numerical model provides an understanding of the contribution of the different forces acting  
190 on the bolted joint make. Fig. 5 presents the different in-plane force components, friction and normal  
191 forces between the various parts of the joint, that add up to the total applied load. The total load  
192 of the joint in Stage I is completely dominated by the friction between the two plates, i.e., without  
193 any contribution from the other forces. At around 0.06 mm displacement, the plates start to slide  
194 (beginning of Stage II) and the contribution from the frictional force between the plates tends to  
195 stabilize without adding any more to the total load. During the sliding stage, when the plates start  
196 to slide, the friction force under the nut increases until the bolt comes in contact with the plate hole.  
197 At 0.15 mm of applied displacement, the bolt comes in contact with the hole to start Stage III, where  
198 the normal force exerted by the bolt on the plates increases. With increased applied displacement, the  
199 bolt undergoes more bending and this results in an increase in the normal force thereby contributing



(a)



(b)



(c)

Figure 4: (a) Load-displacement response of the single lap shear bolted joint showing the different stiffness stages and (b) the evolution of the contact status in the aluminium rib and in the (c) countersunk fastener. (Note: The direction of the applied displacement is indicated in (b) and the initial position of the bolt with zero bending is marked using dashed lines in (c).)

200 to most of the total load on the joint (as seen in Fig. 5). With higher bending of the bolt, there  
 201 is an increased contact area between the bolt and the plate holes, and the friction at the bolt-hole  
 202 interface starts to contribute to the total load. Having said that, the frictional force component in the  
 203 in-plane direction is much smaller when compared to the frictional force in the longitudinal axis of the  
 204 bolt (out-of-plane component) [1]. The sum of these different force components adds up to the total  
 205 applied load on the joint as in Fig. 5.

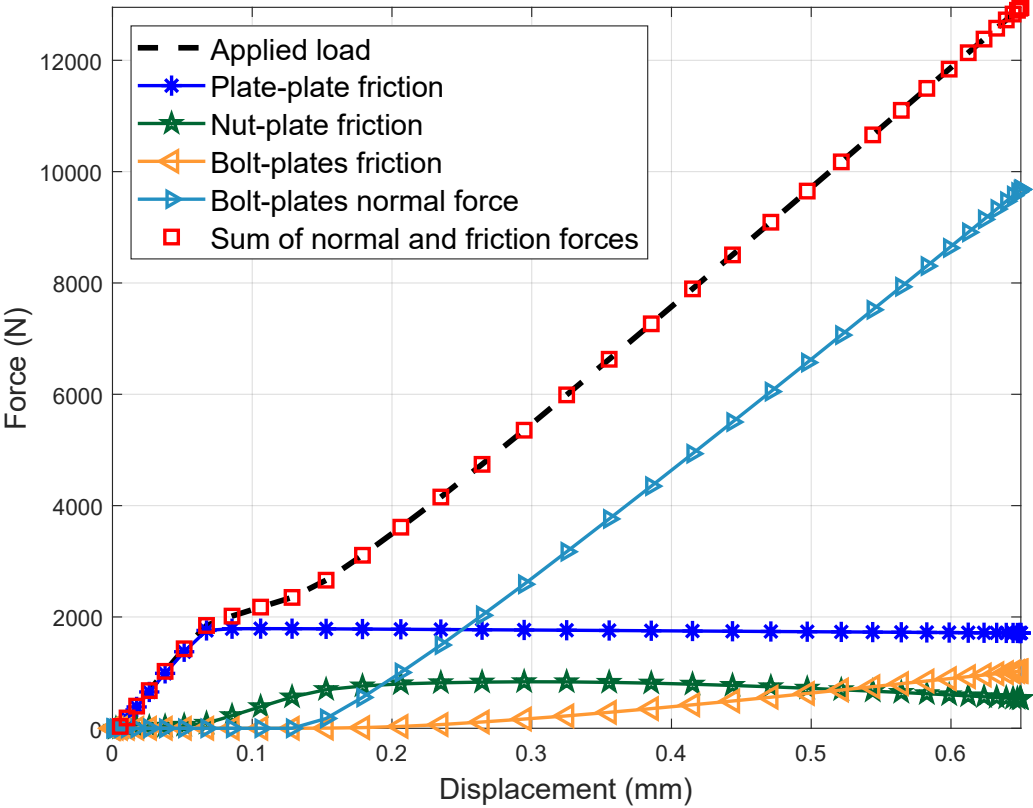


Figure 5: Different load contributions acting on the single lap shear bolted joint in the direction of the applied displacement for the tensile load step.

206 *3.2. Parametric studies*

207 Fig. 6 compares the variation in the bolted joint load-displacement response for the different  
 208 friction coefficients. A higher coefficient of friction signifies that a higher load can be transferred  
 209 through friction between the plates, before the onset of sliding. An increase in the friction values  
 210 characterizes an extended Stage I response and a higher load carrying without any relative motion  
 211 between the plates (3600 N, 1800 N and 900 N for  $\mu=0.6, 0.3, 0.15$ , respectively).

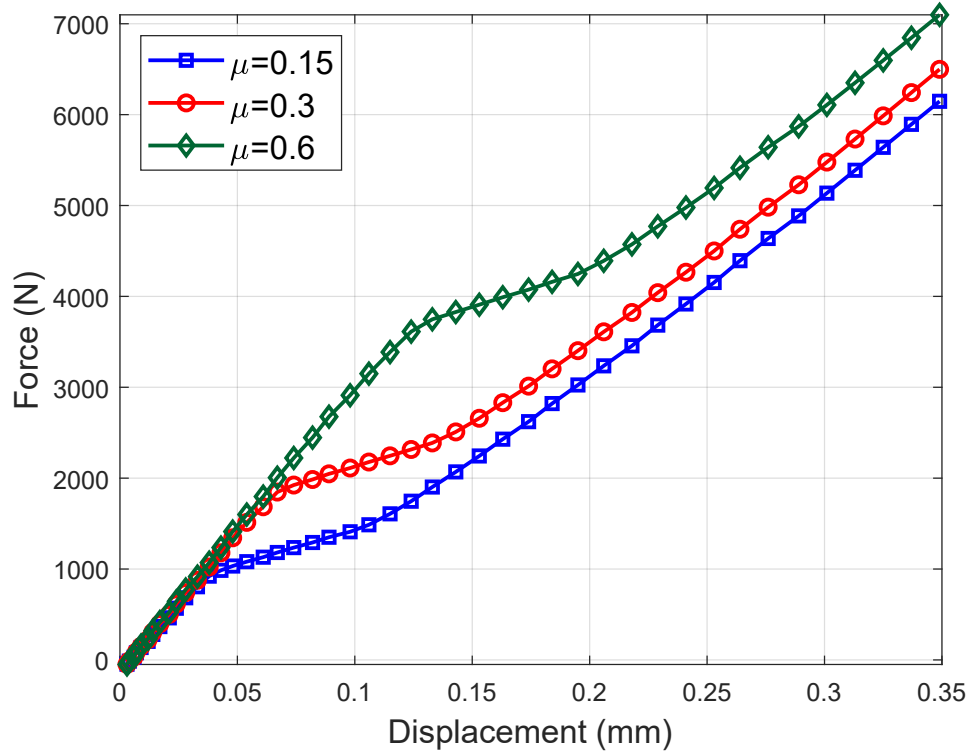


Figure 6: Effect of the coefficient of friction on the load displacement response of the joint behaviour with  $\mu=0.15$ , 0.3 and 0.6.

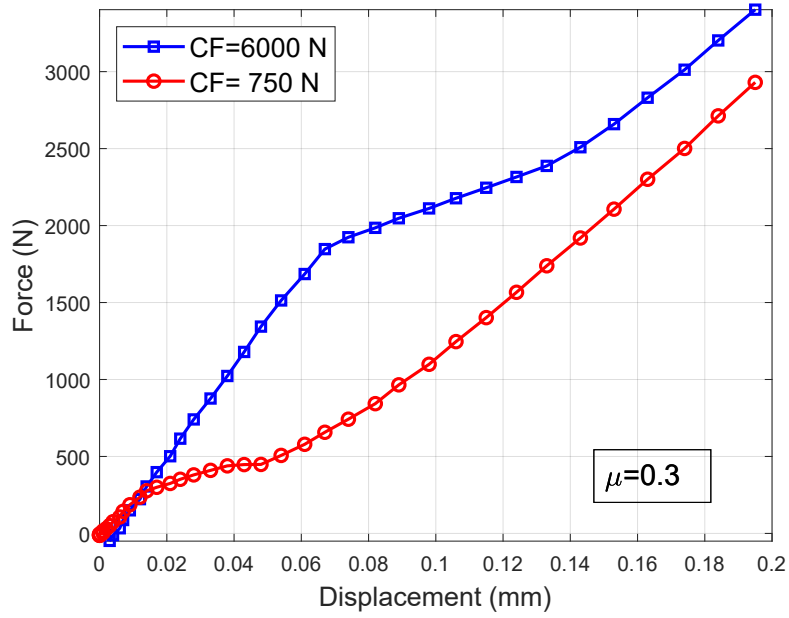
212 A similar trend was seen in the joint response with the variation in the bolt clamping force. Fig.  
213 7 (a) presents the response curves considering two clamping forces (for a standard friction value, 0.3)  
214 and similarly for Fig. 7 (b) but with a lower friction value (0.15). For a reduced bolt clamping force,  
215 the plate sliding (initiation of Stage II) occurs much earlier than that for an increased clamping force.

216 Fig. 8 compares the joint response for two different bolt-hole clearances. The change in clearance  
217 values does not affect the Stage I response, as this stage is completely dependent on the friction and  
218 bolt clamping values. Similarly, the initiation of Stage II is also unaltered with the change in clearance  
219 values, but the extension of Stage II is greatly influenced by the clearance. That is, the larger the  
220 clearance between the bolt and the hole, the greater the sliding between the plates, i.e., before the  
221 bolt comes in contact with the hole. Hence, a higher clearance value delays the onset of Stage III, or  
222 in other words, a delay in the load taken up by the bolt, as seen in Fig. 8. It is also important to note  
223 that there is a reduction (by around 16%) in the stiffness for Stage III for the higher clearance case in  
224 comparison to the lower clearance (Fig. 8). This is due to the difference in the contact area between  
225 the bolt and the hole with respect to the different clearance values. Fig. 9 (a) and (b) illustrate  
226 the development of the contact area within the hole of the aluminium plate for the lower and higher  
227 clearance values, respectively. The figures on the left and right indicate the contact area at the initial  
228 and final point of contact, respectively, between the bolt and the aluminium plate hole. For a higher  
229 bolt-hole clearance, the bolt undergoes further bending before making initial contact, i.e., a reduced  
230 area of contact as well as a reduced joint stiffness when compared to the lower clearance case.

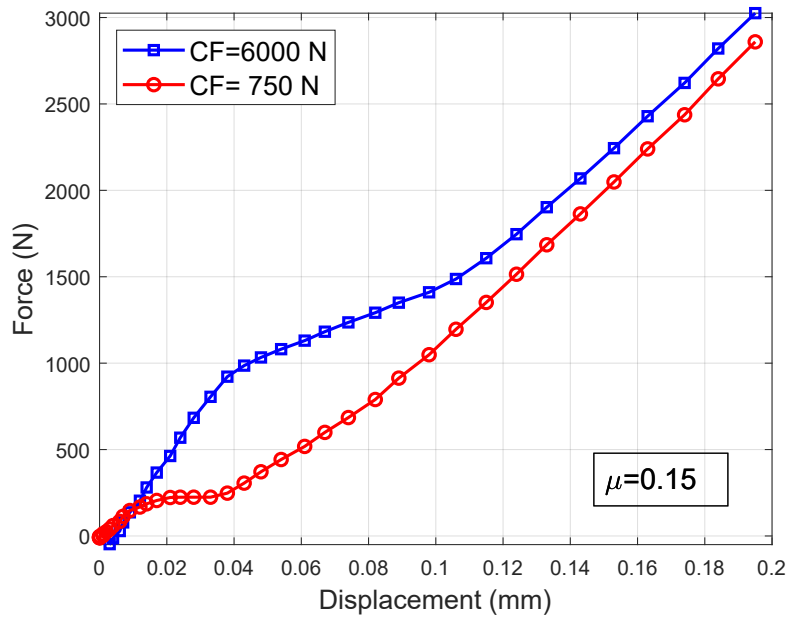
231 Fig. 10 compares the force-displacement response of the joint for different aluminium plate thick-  
232 nesses. The difference in the aluminium thicknesses results in different stiffnesses in Stage I. Compared  
233 to the baseline (6 mm), the thicker case (9 mm) has an 11% increase and the thinner (4 mm) with  
234 a 16% reduction in the stiffness in the stage I (Fig. 10). Apart from the differences in the stiffnesses,  
235 the maximum load attained by Stage I remains the same for all three cases as it depends solely on  
236 the friction and clamping force. The load transferred through friction is independent of the thickness  
237 of the plates. During stage II (sliding), no difference in the response is seen within the cases as the  
238 contribution to the total load is by the frictional force between the nut and the plate (as observed in  
239 Fig. 5). Likewise, the initiation of Stage III occurs at the same applied displacement for the different  
240 cases, but since stage III is characterized by the bolt-hole normal forces, the joint stiffnesses differ for  
241 each case, where the thicker aluminium plate coupon shows the highest joint stiffness.

### 242 3.3. Thermal effects

243 To study the thermal effects on the joint response, we compared the baseline case (with no thermal  
244 step) with two other cases, one with a positive thermal step and the other with a negative thermal  
245 step performed after the preload step and before the tension loading step. Fig. 11 presents the load-



(a)



(b)

Figure 7: Effect of the bolt clamping force on the joint response for a friction coefficient of (a) 0.3 and (b) 0.15.



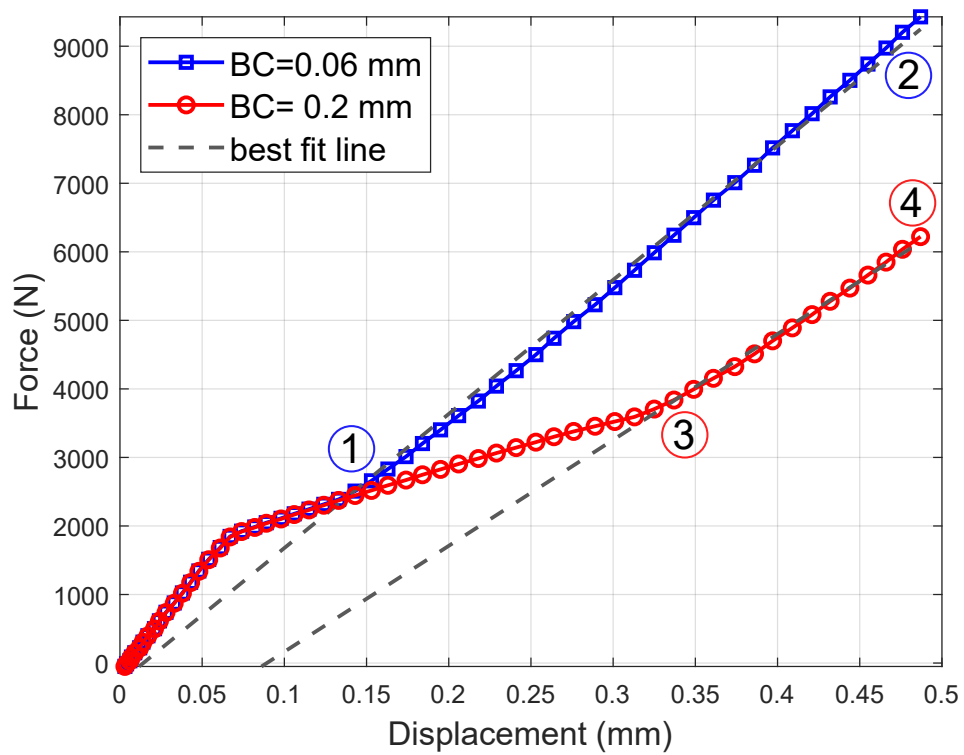


Figure 8: Effect of the bolt-hole clearance on the load displacement response of the joint behaviour. The reduction in the stiffness for Stage III for different bolt-hole clearance values is also shown. Points from 1-4 are used to demonstrate the evolution of contact area for different clearances in Fig. 9.

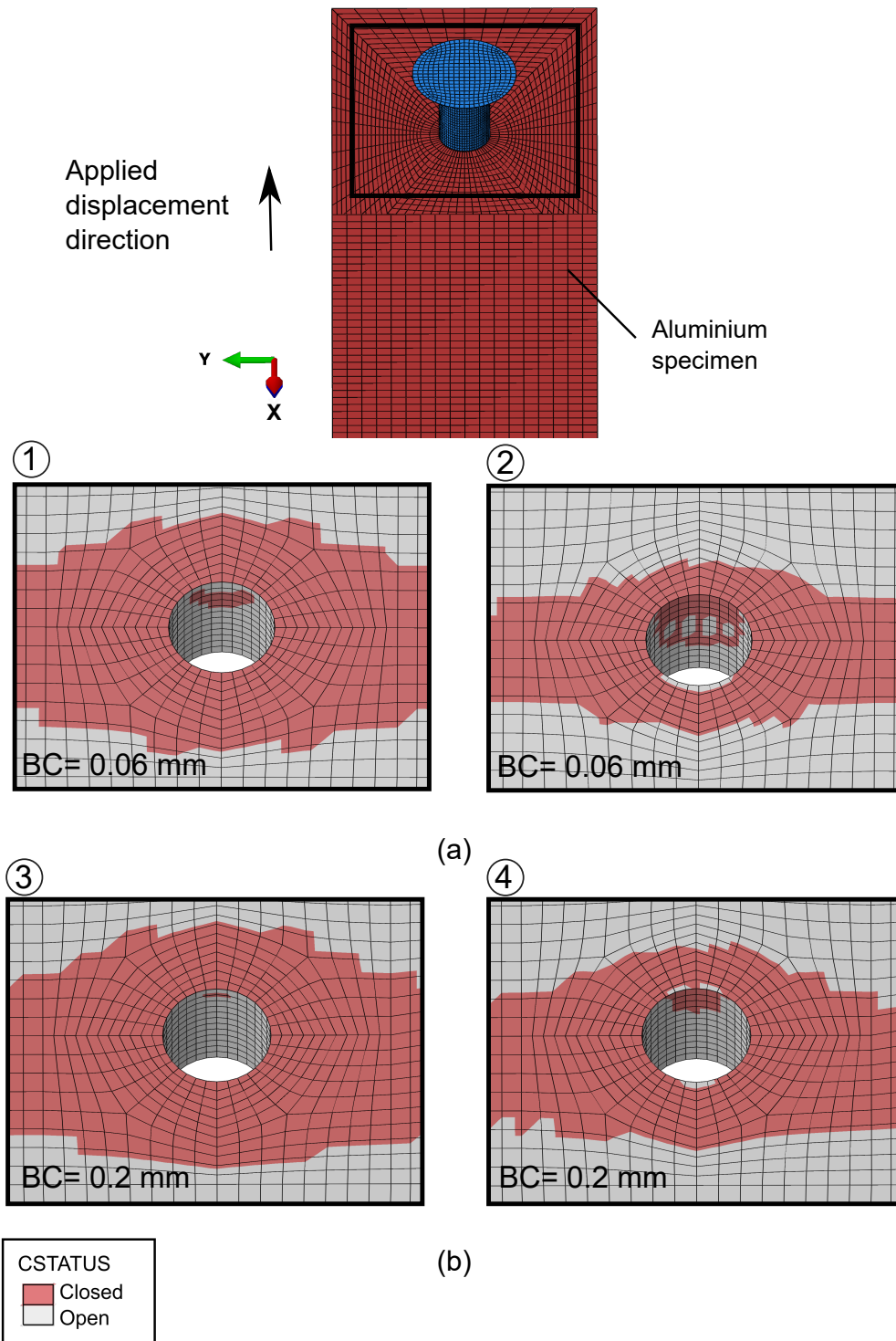


Figure 9: Evolution of the contact area at the hole of the aluminium plate for (a) lower and (b) higher bolt-hole clearance values. The left and right figures denote the initial and final point of contact, respectively, of the bolt with the hole. The top figure illustrates the region of study in the aluminium plate and also the direction of the applied displacement.

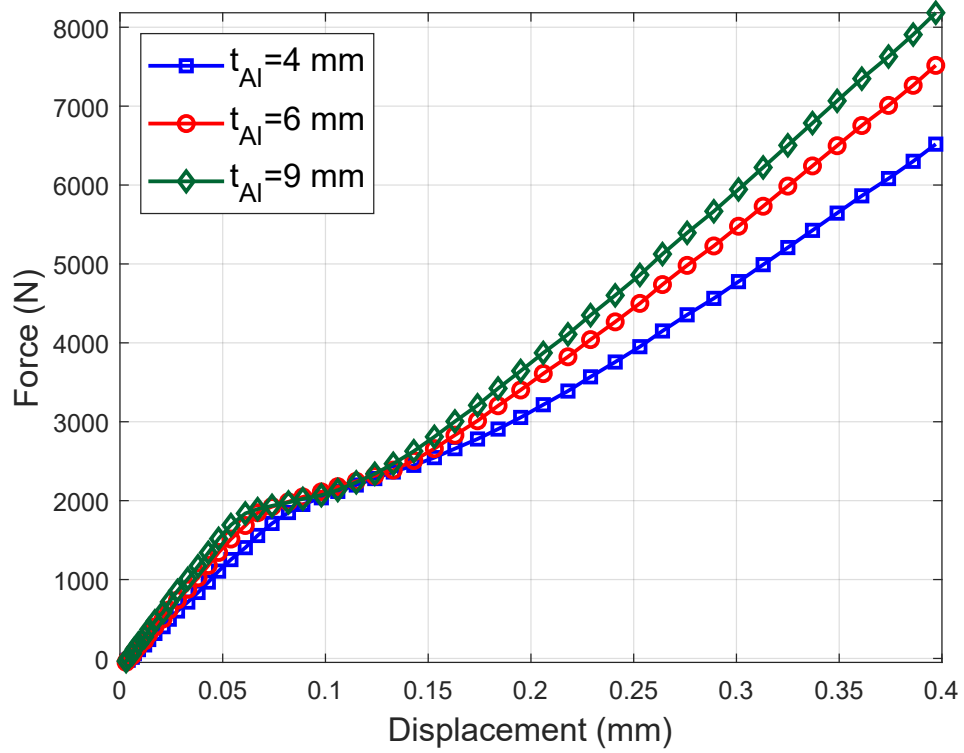


Figure 10: Effect of the thickness of the aluminium plate on the load displacement response of the joint behaviour with  $t_{Al}=4, 6$  and  $9$  mm.

246 displacement response of the joint for the above-mentioned three cases. In the same figure, points A to  
 247 C and A' to C' are also representing, respectively, the beginning and the end of the tensile step for all  
 248 the three cases. Using these points, Fig. 12 a, b, and c compare the development of the bolt contact  
 249 area with the plate hole and bolt bending for the three cases. The response curve of the baseline is  
 250 already explained above in Fig. 4. In Fig. 12, point A shows the status of the bolt before the tensile  
 251 step, and similarly point A' for the end of the tension step. Note that in this figure, the dashed black  
 252 lines denote the initial bolt position to perceive the bolt's bending due to the thermal step.

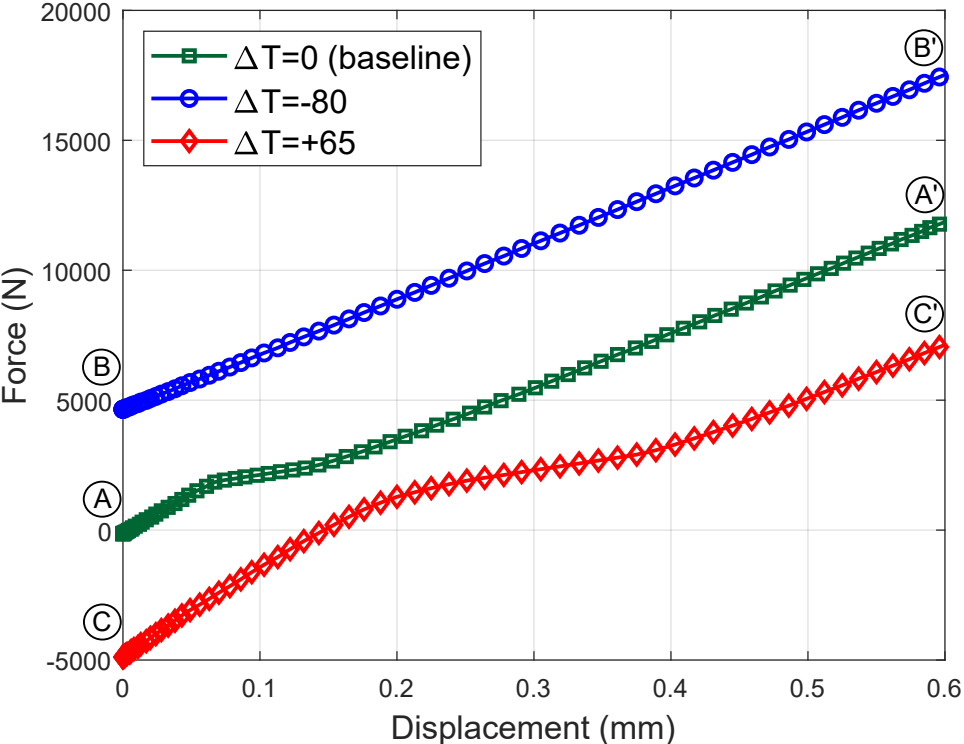


Figure 11: Comparing the load-displacement response of the baseline (without thermal step) with the cases including a positive and negative thermal step.

253 For the baseline, the bolt remains straight before the tensile step; as shown in Fig. 12 (a) in A. At  
 254 the end of the tensile loading, the bolt bends in the counter clockwise direction (in the direction of the  
 255 applied displacement) and we observe high contact of the bolt shaft with the holes (point A' in Fig.  
 256 12). In the case of the negative thermal step prior to the tensile loading, there is a tensile residual  
 257 force of 5000 N at the end of the joint where the displacement is applied. This is due to the fact that  
 258 during a negative thermal case, the whole joint contracts, and since the assembly is clamped at the  
 259 ends, there is a positive reaction force at the joint end. The curve for the negative case, unlike the  
 260 other cases, exhibits a single stage stiffness curve from the beginning to the end of the loading (Fig.

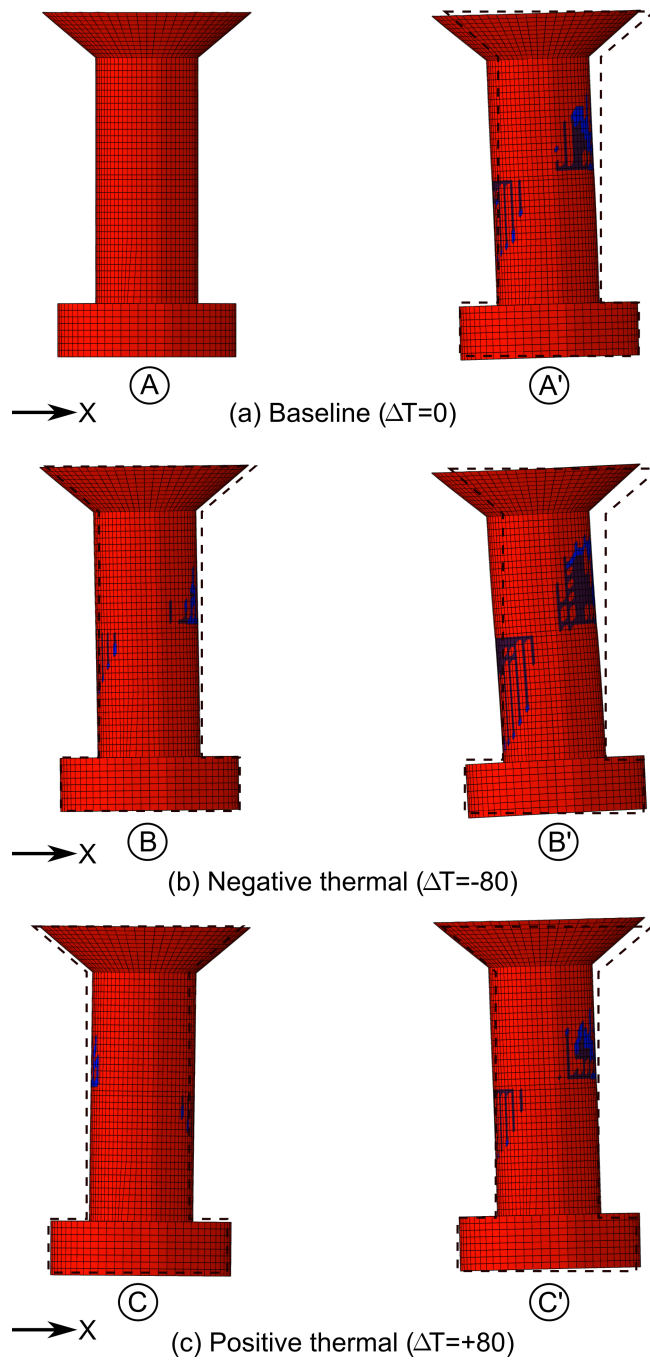


Figure 12: Development of contact area and bolt bending during the tensile loading, where the images on the left and right denote before and after tensile loading. Note that the displacement is applied in the negative X direction and the initial position of the bolt with zero bending is shown using dashed lines.

261 11). This is explained in the Fig. 12 as, due to negative thermal step, the aluminium at the bottom  
262 contracts more than the CFRP and the steel bolt, leading to the bolt bending in the counter clockwise  
263 direction. Hence, at the end of the thermal step, the bolt shaft is already in contact (for the given  
264 bolt-hole clearance value) as seen at point B. Further on during the tension step, the displacement is  
265 applied to the joint in the negative X direction, the bolt rotates further in this direction, thus creating  
266 a greater contact with the plate hole as seen at point B'. Thus, the single stiffness stage seen with  
267 the negative case in Fig. 11 is the joint stiffness when the bolt shaft is in contact with the hole. In  
268 addition, note that for all the above presented curves, the high magnitude of load is not realistic, as  
269 while considering damage, the final failure might have happened before reaching these high load levels.

270 A reverse phenomenon is noticed for the positive thermal case, as at the end of the thermal step, the  
271 joint expands and creates a compressive reaction force at the joint end (as in Fig. 11). Contrary to the  
272 negative thermal, the joint expands due to the positive thermal jump and the aluminium plate expands  
273 more than the CFRP and steel, leading to the bolt bending in the clockwise direction as seen in Fig.  
274 12 (c) at point C. During tensile loading (applied in the negative X direction), the bolt bends back  
275 in the counter clockwise direction as seen in C' in Fig. 12. This is observed in the force-displacement  
276 response in Fig. 11 for the positive thermal case with three stiffness stages, where the first one refers  
277 to the joint stiffness when the bolt is in contact with the plates (as in C in Fig. 12). With applied  
278 displacement, the bolt rotates back to its initial position and gradually loses contact with the plate  
279 hole. In the second stage, the bolt is no longer in contact with the hole, hence the low stiffness in this  
280 stage. Further, with increased loading, the bolt swings to the direction of applied displacement and  
281 makes contact with the plate hole (point C' in Fig. 12), leading to the third stage in the curve.

282 Fig. 13 (a) presents the evolution of the bolt clamping force during the steps considered for the  
283 baseline (without thermal step), and the cases with positive and negative thermal steps included. Fig.  
284 13 (b) shows the contact status between the plates at different time frames of the thermal load. During  
285 preload, the bolt undergoes tension to clamp the plates together. As seen in Fig. 13 (a), at the end  
286 of the preload step, the bolt force reaches the pre-defined value of 6000 N. A circular sticking contact  
287 region between the CFRP-aluminium interface demonstrates the clamping of the plates (Fig. 13 (b)).

288 During the negative thermal step, the plates contract more than than the steel bolt in the thickness  
289 direction, leading to a reduction in the bolt clamping force by around 40% when compared to the initial  
290 preload value. This loosening of the bolt is critical as it reduces the further load carrying capability of  
291 the joint [2]. Conversely, the positive thermal case induces a higher expansion in the plates compared  
292 to the bolt, thereby leading to an increase in the bolt clamping force by around 20%. A positive  
293 thermal case poses the threat of over-stressed bolts and possibilities of surpassing the yield stress of  
294 the bolt material. We observe sliding in both thermal cases (at step time 1.5 s in Fig. 13 (b)), but  
295 there is a clear difference in the contact profile and area between the negative and positive cases. At

296 the end of the thermal step, the positive thermal still holds a uniform contact zone around the bolt,  
297 whereas the contraction of the plates in negative thermal step has caused a reduction in the contact  
298 zone (at step time 2.0 s in Fig. 13 (b)).

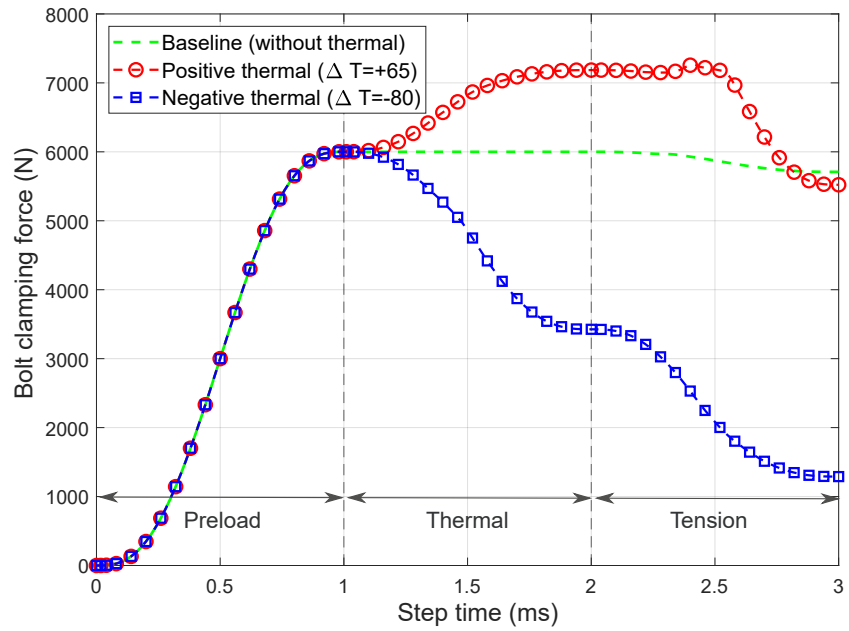
299 Further on during tensile loading, both thermal cases caused a reduction in the clamping force  
300 of the bolt, due to the shear sliding of the plates. In particular, the negative thermal case is more  
301 critical as the clamping force of the bolt is reduced to around 1000 N (compared to 6000 N and 3500  
302 N, respectively, at the end of the preload and thermal steps) after the tensile loading. The drastic  
303 reduction in the bolt's clamping force when compared to the baseline case, demonstrates the effect  
304 that a negative thermal load can have on a torqued bolt.

305 Fig. 14 presents the relative shear sliding between the plates for both thermal cases. This was  
306 calculated from the relative difference in the in-plane displacements from the two nodes. A maximum  
307 shear sliding of 0.2 mm was recorded for the negative thermal case, which is critical enough to counter-  
308 act the bolt-hole clearance and initiate contact between the bolt and the plates during a temperature  
309 difference (as seen in Fig. 12 (b) and (c)). An increase in temperature induces joint expansion and  
310 at the overlapping region of the dissimilar materials (as in Fig. 3(a)), the aluminium plate displaces  
311 in the negative X direction and CFRP in the positive X direction. The higher thermal expansion  
312 coefficient of aluminium has resulted in a four-fold higher in-plane displacement value when compared  
313 to the CFRP plate. A similar trend is seen with the negative thermal case, but in the reverse. During  
314 tensile loading, both the plates displace towards the negative X direction (direction of the applied  
315 displacement). The CFRP plate displaces more as the tensile loading was applied at the CFRP side  
316 of the assembly.

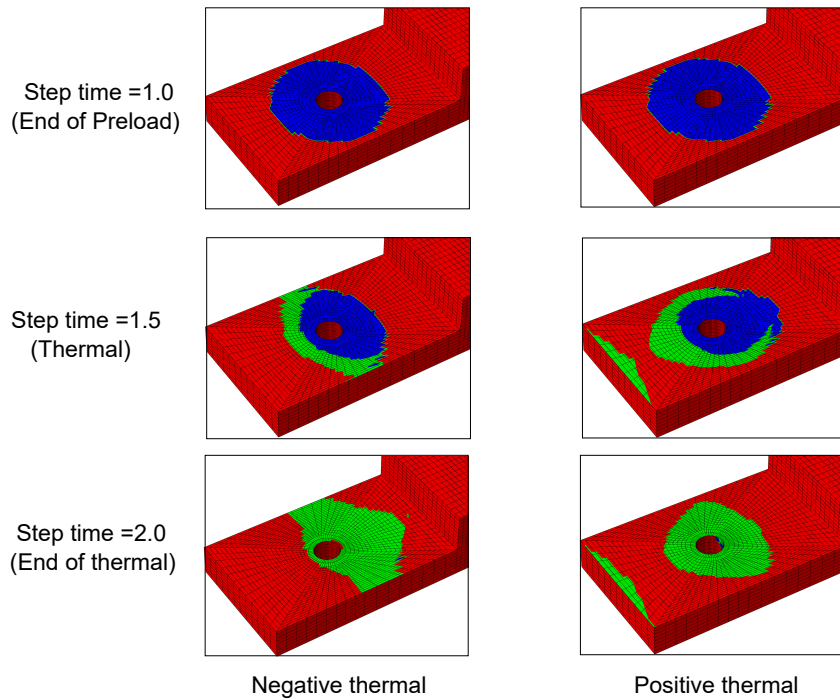
### 317 3.4. Loading-Unloading-Reloading cycle

318 We simulated a loading, unloading and reloading loop on the baseline case to study the joint  
319 response and evolution of contact regions. Aircraft experience a similar scenario but obviously in a  
320 higher number of cycles. Fig. 15 (a) presents the load-displacement response of the bolted joint for a  
321 loading, unloading and reloading loop. The joint is loaded until a displacement of 0.35 mm and then  
322 unloaded completely to a zero displacement. Further, the joint is reloaded by applying a displacement  
323 until 0.5 mm. We have selected different points in the joint response to study the contact evolution  
324 at different regions in detail. Fig. 15 (b) presents the contact tracking for the plate interface and the  
325 countersunk fastener for all the selected points throughout the loop. Fig. 16 presents the contribution  
326 of all the different forces (frictional and bearing force) that sums up to the total force during the whole  
327 loading-unloading-reloading cycle.

328 We explain the scenario by detailing each point as following:



(a)



(b)

Figure 13: (a) Comparison of the evolution of bolt clamping force for the baseline (without thermal) and with thermal (positive and negative) cases. Note that the baseline does not have a thermal step and hence the value is kept constant. (b) Evolution of contact status at the plate interface during negative and positive thermal (note that the blue contour indicates closed (sticking) status and green indicates sliding).



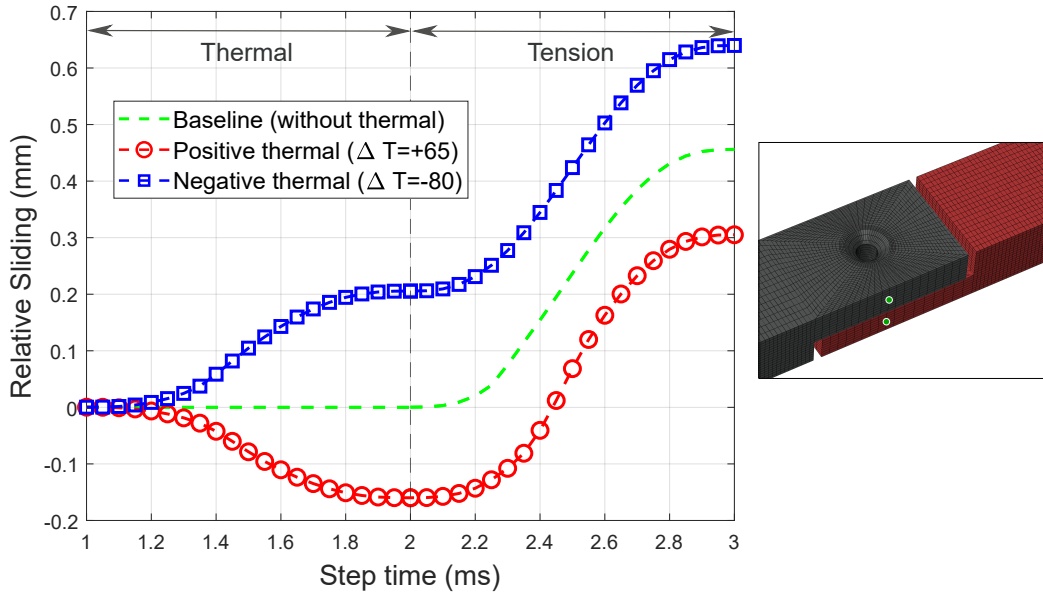


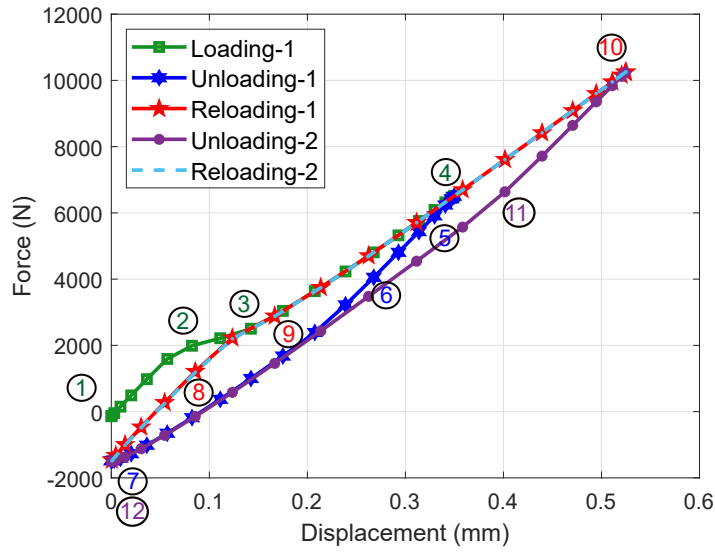
Figure 14: Shear sliding between the aluminium and CFRP plates for negative and positive thermal cases. (Note that the shear sliding was measured as the difference in the in-plane nodal displacements in the X direction measured at two nodes (marked in green circles) at the edge of each part at the center of the assembly, as shown in the sub-figure)

329 1: End of preload and beginning of tension step. Sticking contact zone at the plates' interface  
 330 and at the aluminium plate-bolt nut interface.

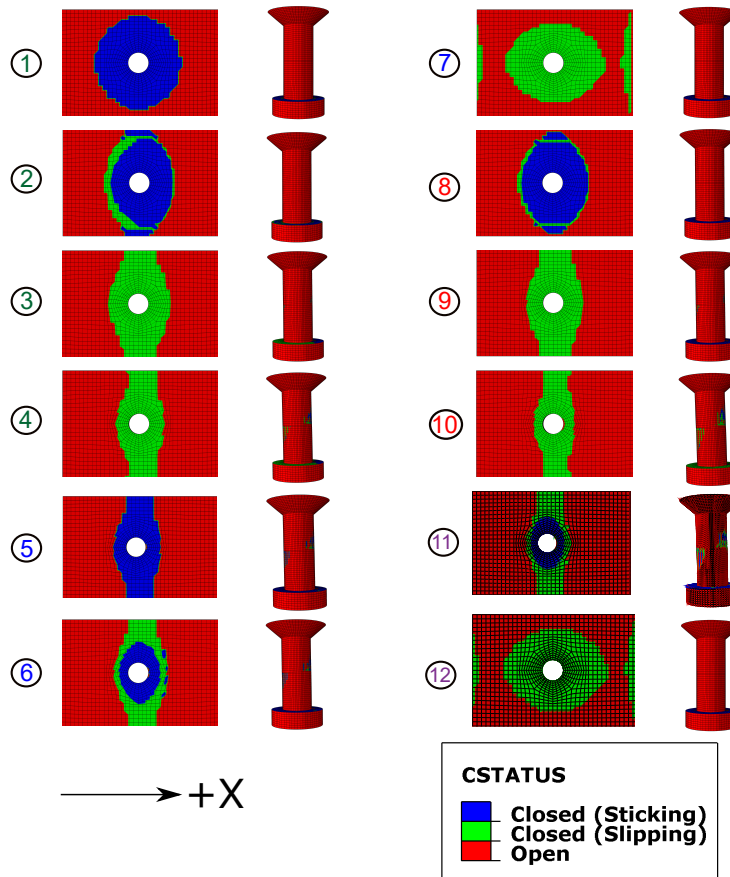
331 2: End of stage I (characterized by friction) and beginning of stage II (sliding phase). At the  
 332 end of stage I, the total reaction force equals the frictional force and hence the plates start to  
 333 slide. The upper plate moves in the direction of the applied displacement (negative X direction)  
 334 and the resulting frictional force acts in the positive X-axis (as shown in Fig. 15). Until point 2,  
 335 total force is completely contributed by the plate-plate friction (see Fig. 16).

336 3: End of stage II and beginning of stage III, where there is complete sliding between the plates  
 337 (all slipping region in Fig. 15 (b) point 3)) and initiation of contact between bolt shaft and the  
 338 holes. Slight bolt rotation in the direction of applied displacement which leads to sliding and  
 339 sticking at the plate-bolt nut interface. Plate-bolt bearing force starts to contribute to the total  
 340 force as seen in Fig. 16.

341 4: Last point in the loading phase. Higher sliding between the plates and a reduced contact area  
 342 compared to point 3. Higher contact between the bolt-shaft and holes and higher bolt rotation  
 343 (compared to 3). As seen in Fig. 16, most of the contribution to the total force is from the  
 344 plate-bolt bearing force due to the high contact and from the plate-plate friction force which  
 345 remains constant from point 2 to point 4.



(a)



(b)

Figure 15: (a) Loading, unloading and reloading response of the single lap shear hybrid bolted joint and (b) Contact status at the aluminium plate and the countersunk bolt for selected points in the curve (note that the blue contour indicates closed (sticking) status and green indicates sliding)).

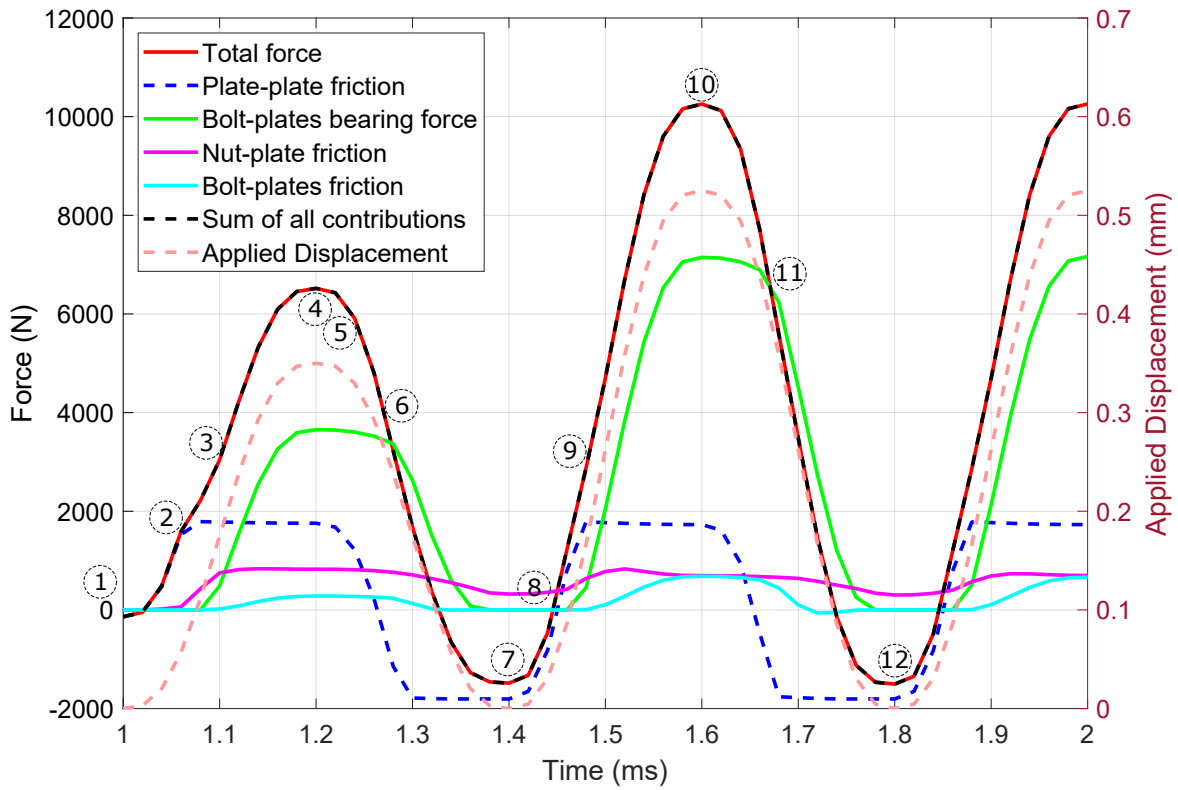


Figure 16: Evolution of total force (left Y axis) and displacement (right Y axis) with respect to time (X axis) during the whole loading-unloading and reloading cycle. Different force contributions (frictional forces and bearing forces) that sum up to the total force are also presented.

346 5: Beginning of the unloading phase. At this point of reversing the direction of the displacement,  
347 the displacement rate is null, and as a consequence, there is no sliding between the plates, shown  
348 by complete sticking in point 5 in Fig. 15 (b). At this point, the closed contact keeps contributing  
349 with a frictional force in the direction of the positive X-axis.

350 6: During unloading phase. When unloading starts (applied displacement direction is reversed), a  
351 fraction of the contact surface starts to slide, building a frictional force in the negative X-axis. At  
352 the same time, the closed area still contributes in the positive X direction. (Point 6 in Fig. 15 (b)  
353 shows both sticking and sliding regions in the contact area). Note that the bearing force between  
354 plate-hole and bolt shows a plateau during unloading (between  $t=1.2$  to  $t=1.28$  ms in Fig. 16),  
355 as a consequence of the contribution of the closed contact restricting the local displacement of  
356 the plate. This is understood as frictional hysteresis. During the transition from point 5 to 6,  
357 the fraction of sliding area increases while the closed contact decreases, hence the total frictional  
358 force grows in the negative X direction. At point 6 ( $t=1.275$  ms,  $d=0.28$  mm), the frictional  
359 force reaches zero as the contribution of the closed and sliding contact areas compensate with  
360 each other.

361 7: End of unloading phase. From point 6 to point 7, the sliding between the plates has increased,  
362 where the upper plate is moving to the positive X direction. Hence, a negative total force builds  
363 up as a consequence of the friction force (in the negative X direction), causing the observed  
364 compression total force at zero displacement (point 7 in Fig. 15 (b) or  $t=1.4$  ms in Fig. 16).  
365 Bolt returns to the origin and hence no contact between the bolt and the plates, therefore a zero  
366 bearing force at point 7 (Fig. 16).

367 8: First point of reloading phase. Transition from point 7 to 8 is similar to the transition from  
368 point 4 to 5 but in the other direction. Total force and the plate-plate frictional forces are almost  
369 zero as seen in Fig. 16.

370 9: Second point in the reloading phase. The reloading curve joins the loading curve and similar  
371 response to point 3 in loading phase. Initiation of contact between bolt shaft and holes.

372 10: Highest displacement applied, extensive sliding and reduced contact surface between the  
373 plates. High contact of the bolt shaft and high bolt rotation. Close to complete slipping at the  
374 plate-bolt nut interface.

375 11: Point at the end of the first stage of unloading-2, where the friction force acts in the opposite  
376 direction (as explained in point 6).

377 12: Point of zero displacement in the second unloading loop. Same compressive total force as in  
378 point 7. At zero displacements, the total force is contributed solely by the plate-plate friction (in  
379 the negative X direction). The plate-plate frictional force remains the same at the end of each  
380 unloading stage, as it depends on the bolt preload which is retained to the initial preload value  
381 at the end of each unloading cycle. (see Fig. 16).

382 This study addressed the preliminary understanding towards the behaviour of a bolted joint with  
383 dissimilar materials under thermal and mechanical loads. With the key findings from this coupon level  
384 study, the next step in the framework of this project is to move to the sub-component level where we  
385 simulate the thermal response of a wing box sub component made of a single aluminium rib bolted  
386 to CFRP skin and spars using countersunk fasteners. Further, the ultimate objective is to model and  
387 simulate an entire hybrid wing box comprising of four different materials, to study the deformations  
388 arising from the thermal jumps.

#### 389 4. Conclusion

390 In the quest to reduce weight, aircraft industries are combining metallic and lightweight carbon  
391 components in their primary structures. Aircraft structures with such hybrid joints, where the plates  
392 are made of dissimilar materials that expand differently with temperature, have shown signs of dam-  
393 age at the joint due to over stress and different responses at extreme temperatures. Hence, in this  
394 study, using a detailed 3D finite element model, we investigated the response of a hybrid bolted joint  
395 under thermal and mechanical loads. We simulated a single lap shear composite-aluminium joint with  
396 countersunk fastener using bolt preload, thermal jump and static tensile loading steps. Under me-  
397 chanical tensile load, the joint response exhibits different stiffness stages characterized as ‘No sliding’,  
398 ‘Sliding’ and ‘Contact’. Out of the different joint parameters studied, bolt-hole clearance exhibits a  
399 high influence in the sliding stage and determines the contact area between the hole and the plate. A  
400 higher out-of-tolerance clearance can impose a reduction in the joint stiffness, by around 16%, and also  
401 increased bolt bending and contact area. The coefficient of friction and bolt clamping force parameters  
402 only influenced the ‘No sliding’ stage. Further, we presented how thermal loading can significantly vary  
403 the bolt preload (40% reduction and 18% increase in bolt preload under negative and positive thermal  
404 conditions, respectively). In addition, a tensile load followed by a negative thermal step reduced the  
405 bolt preload by 85% compared to a baseline case with no thermal change. This drastic change can lead  
406 to bolt loosening (negative thermal) or over-stressed bolts (positive thermal), leading to a reduction  
407 in the load carrying capacity of the joint.

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414 other than the Union.

## 415 **Data Availability**

416 The raw/processed data required to reproduce these findings cannot be shared at this time due to  
417 legal or ethical reasons.

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