

EFFECTS OF VARIABLE AMPLITUDE FATIGUE ON DELAMINATION AND CRACK GROWTH RATE MODELS

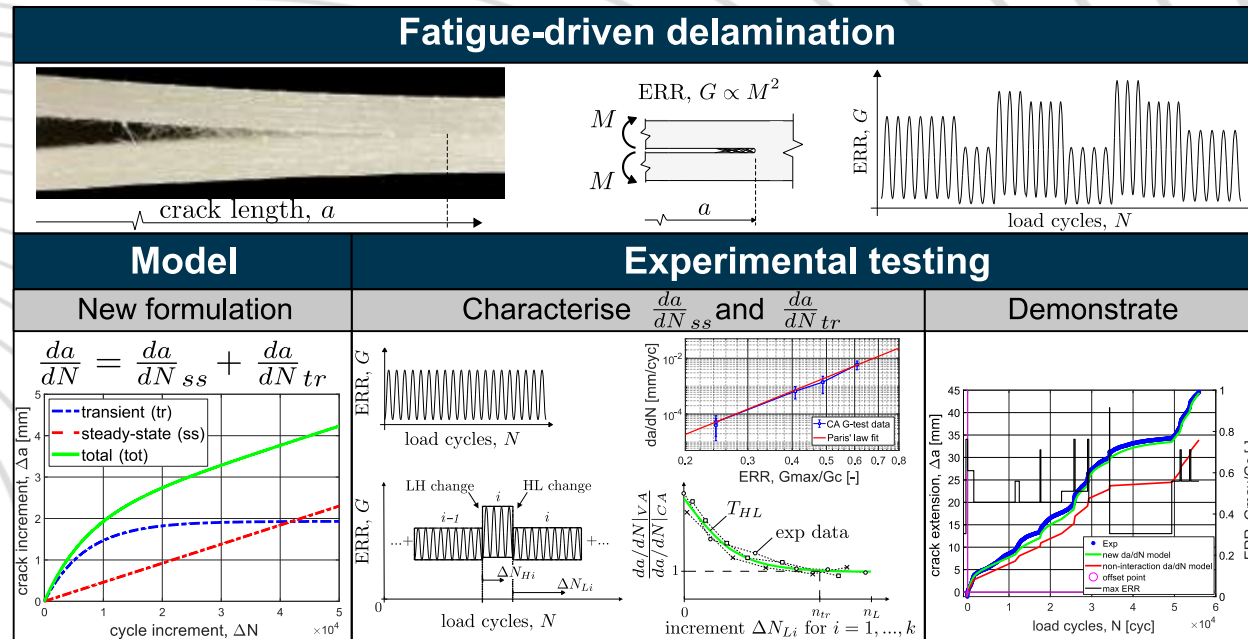
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Jensen SM, Bak BLV, Bender JJ, Carreras L & Lindgaard E (2021) *Transient delamination growth in GFRP laminates with fibre bridging under variable amplitude loading in G-control, Composites Part B: Engineering* 225: 109296

Jensen SM, Carreras L, Bak BLV, Lequesne C & Lindgaard E (2023) *A crack growth rate model with load history effects for mode I fatigue-driven delamination under multi-level block loading, International Journal of Fatigue* 172(4): 107595

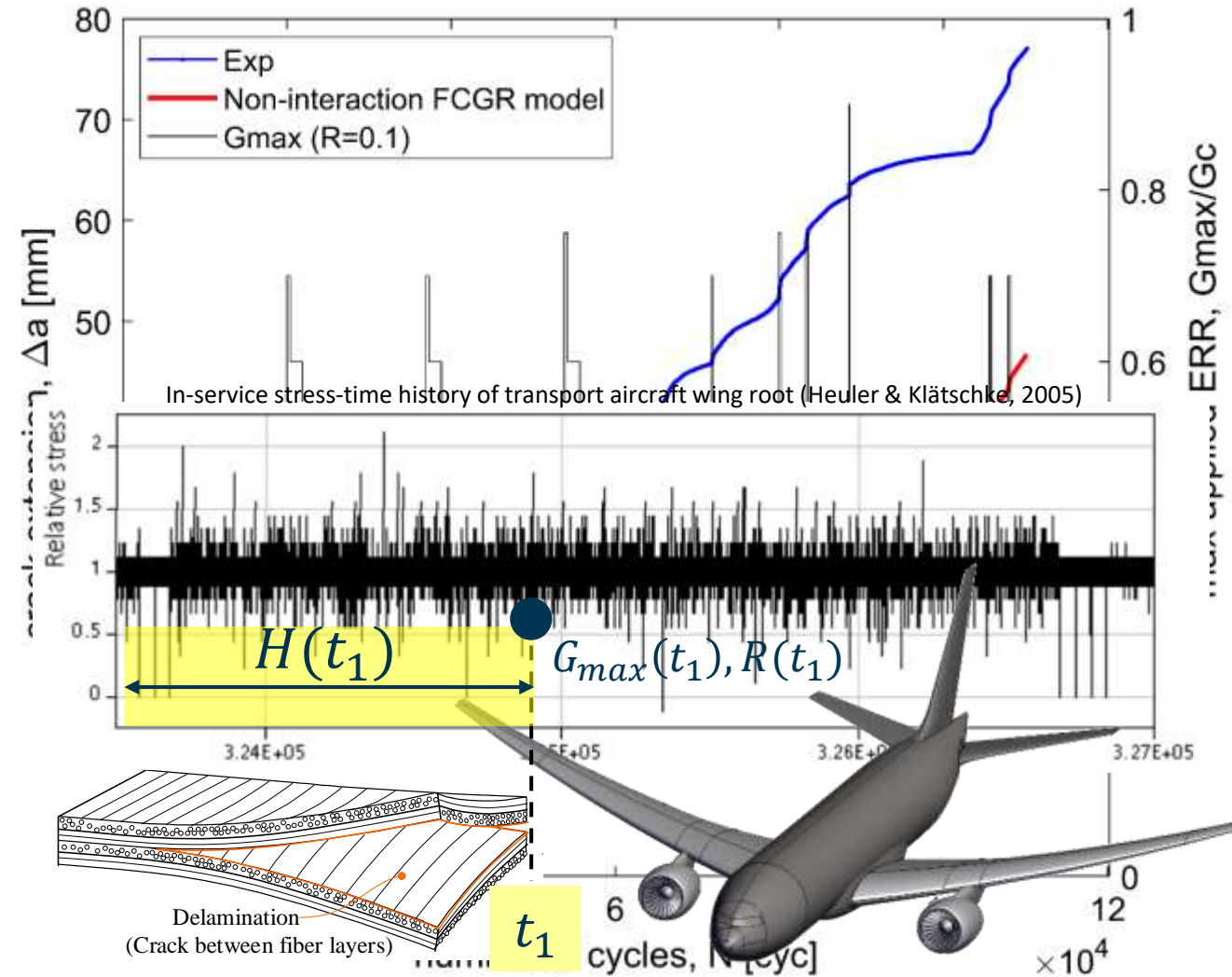
Background and research objective

- Delaminations in FRPs may propagate under **VA fatigue** during operation
- In crack growth rate (**CGR**) models the loads are expressed in energy release rate (ERR) values:

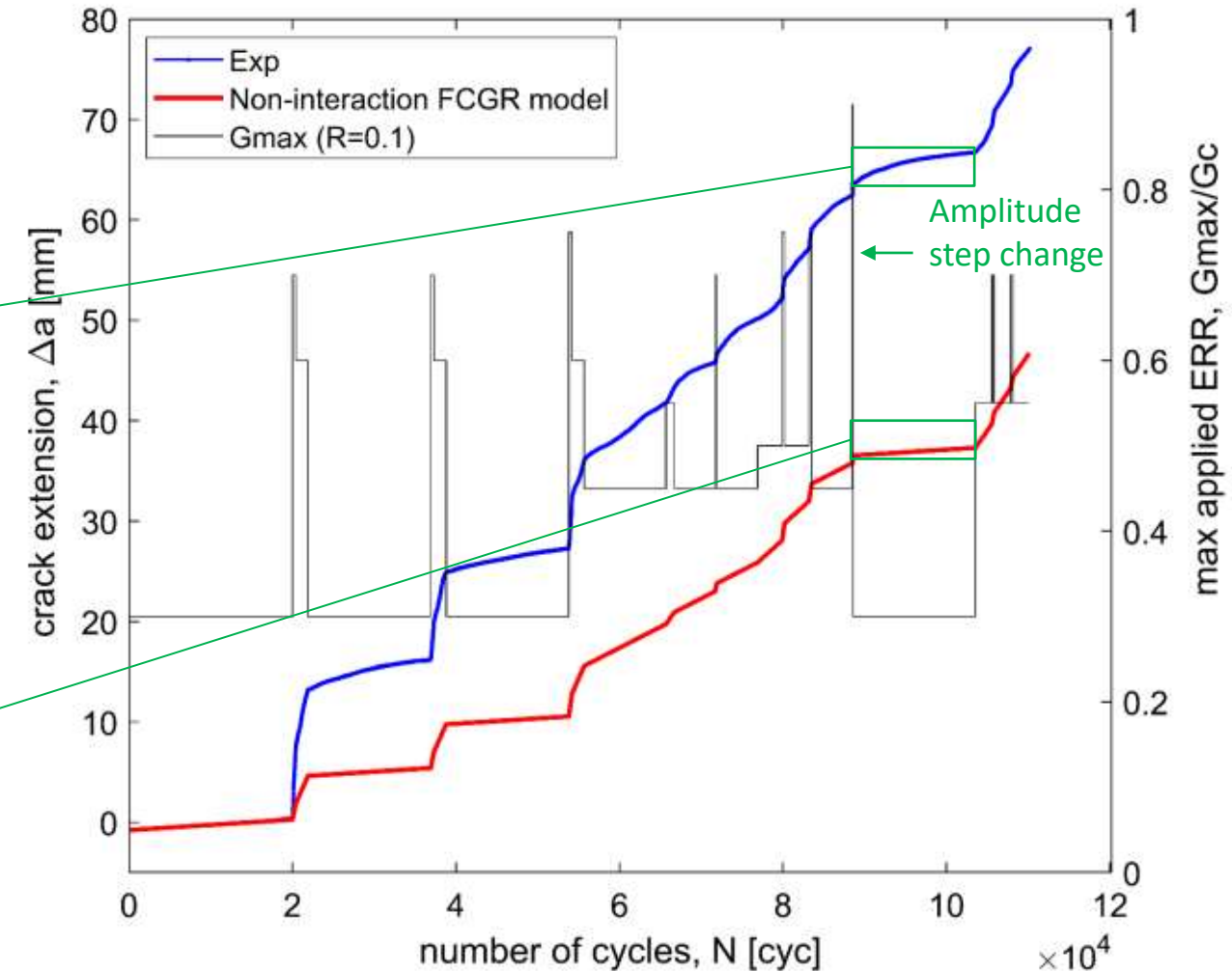
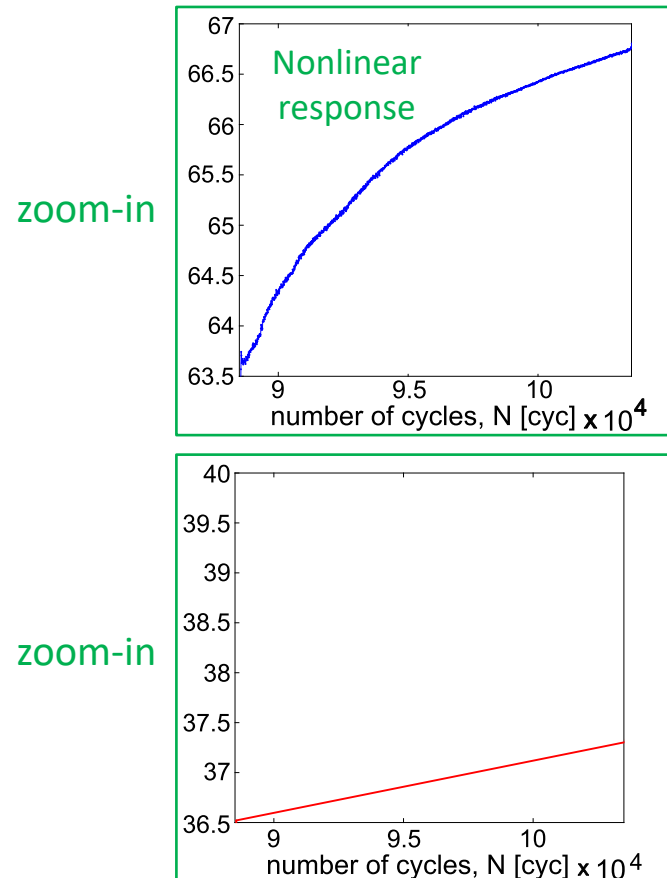
$$\frac{da}{dN}(t_1) = f(\underbrace{G_{max}(t_1), R(t_1)}_{\text{Non-interaction model}}) \overset{?}{H(t_1)}$$

- How is the crack growth rate (da/dN) affected by the load history (H)?

VA example:



- Concentrate on the crack growth following **amplitude step changes** because of interesting **phenomenological behaviors**



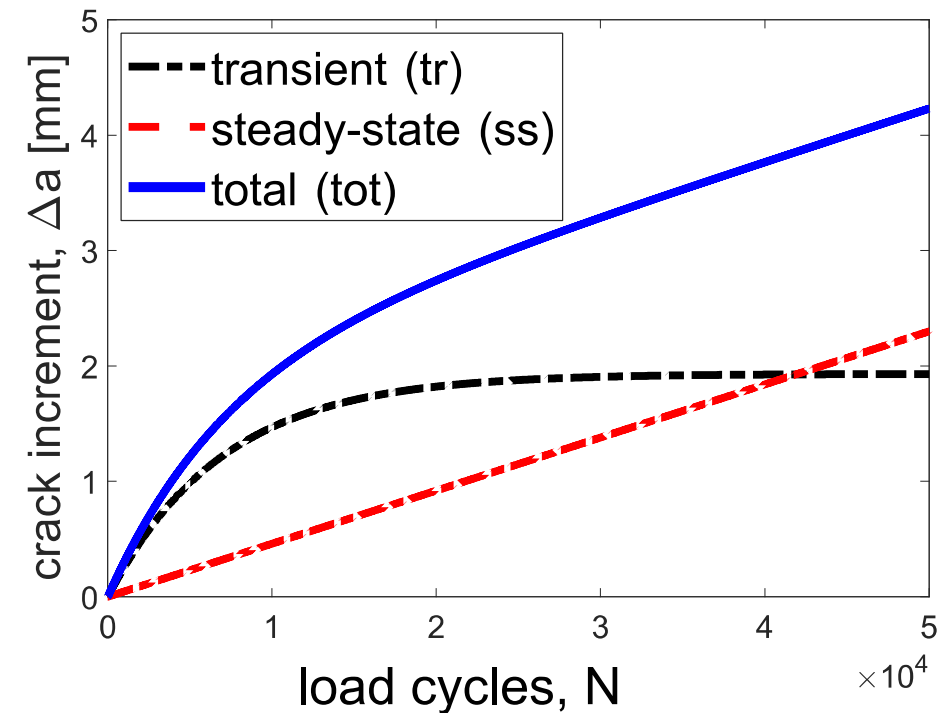
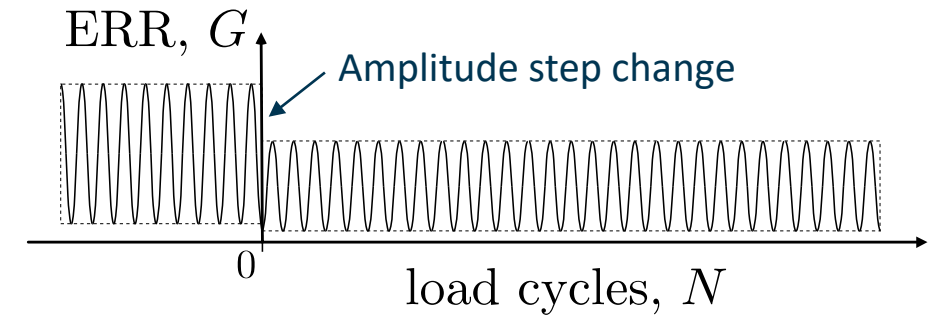
Background and research objective

- Can the **nonlinear experimental response** be decomposed into a **steady-state** and **transient** response?

- A new CGR model:

$$\frac{da}{dN} = \underbrace{\frac{da}{dN_{ss}}}_{\text{Steady-state}} + \underbrace{\frac{da}{dN_{tr}}}_{\text{transient}}$$

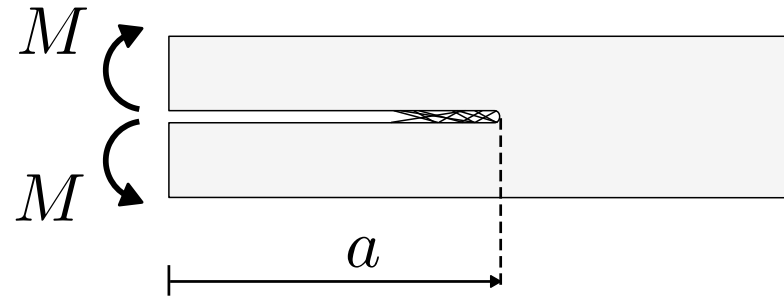
- Questions: How...
 - can the responses (ss, tr) be **characterized**?
 - to **formulate** these with CGR functions?
 - will the new model **perform** under VA fatigue?



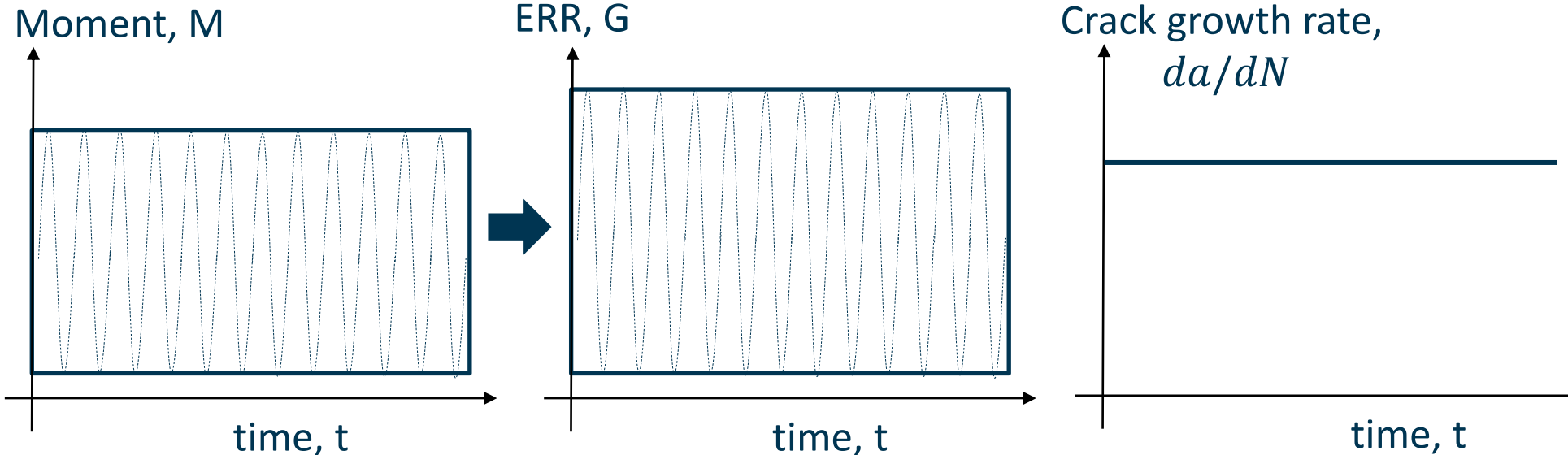
Cyclic steady-state crack growth

Pure moment loaded DCB specimen:

- ERR-controlled testing is possible
- Constant amplitude (CA) ERR-testing enables “cyclic steady-state crack growth”
- Constant crack growth rate



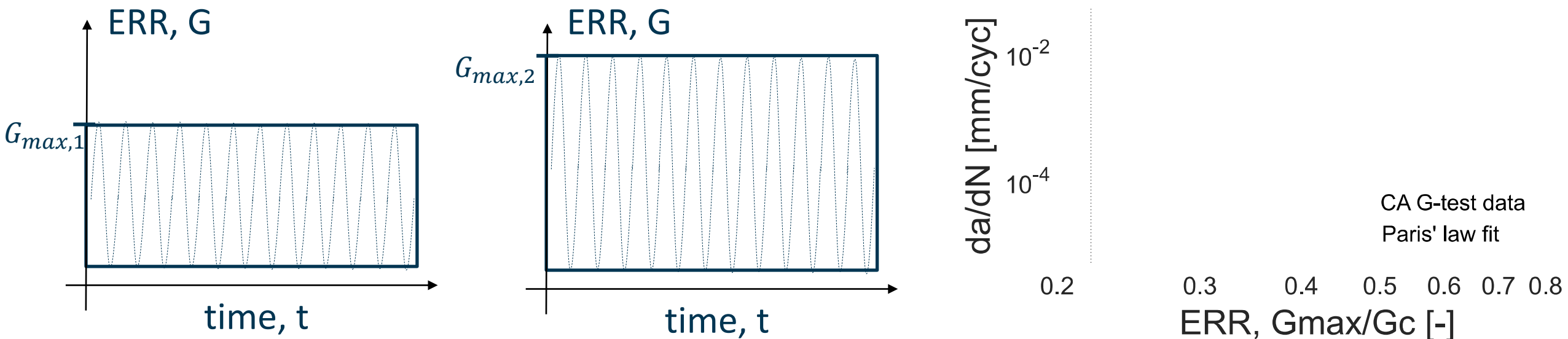
$$G = \frac{M^2}{bEI}$$



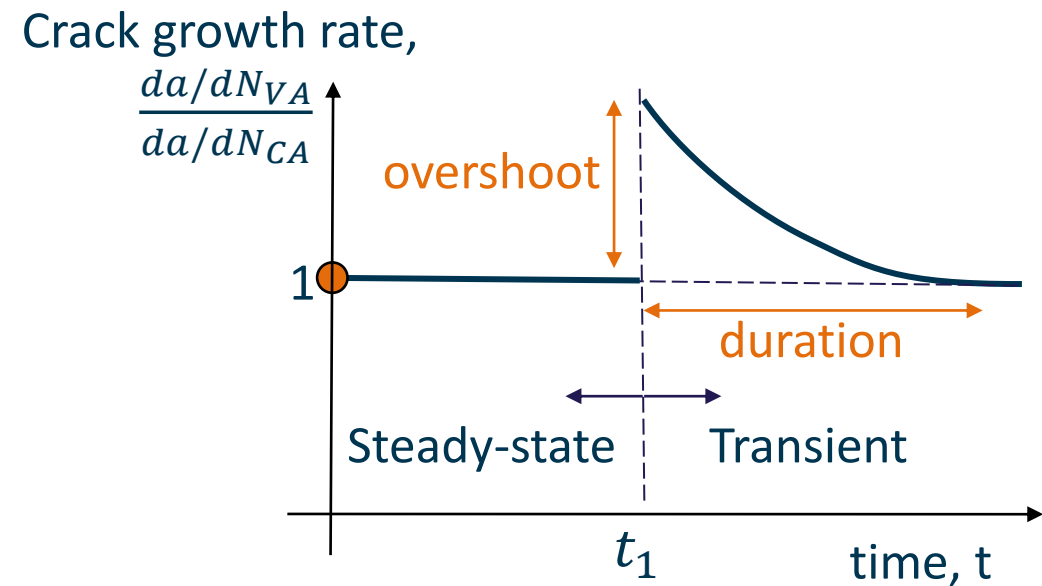
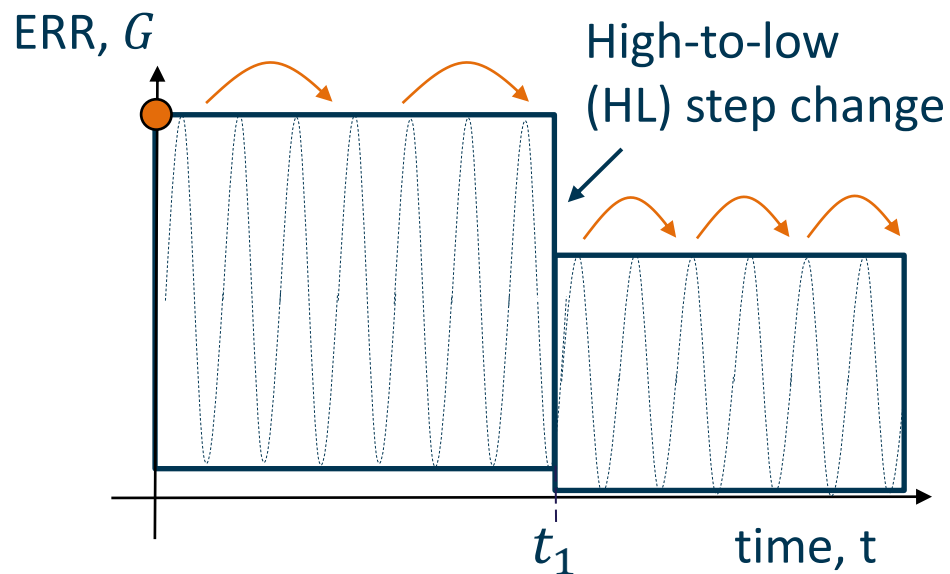
Cyclic steady-state crack growth characterization

- Use the CA ERR-tests to characterize the steady-state term: $\frac{da}{dN} = \frac{da}{dN_{SS}} + \frac{da}{dN_{tr}}$
- Multiple CA tests are conducted at different levels of G_{max}

- A Paris' law like relation: $\frac{da}{dN_{SS}} = F_{SS}(G_{max}, R)$ ← Identical to conventional CGR models and neglects the load history

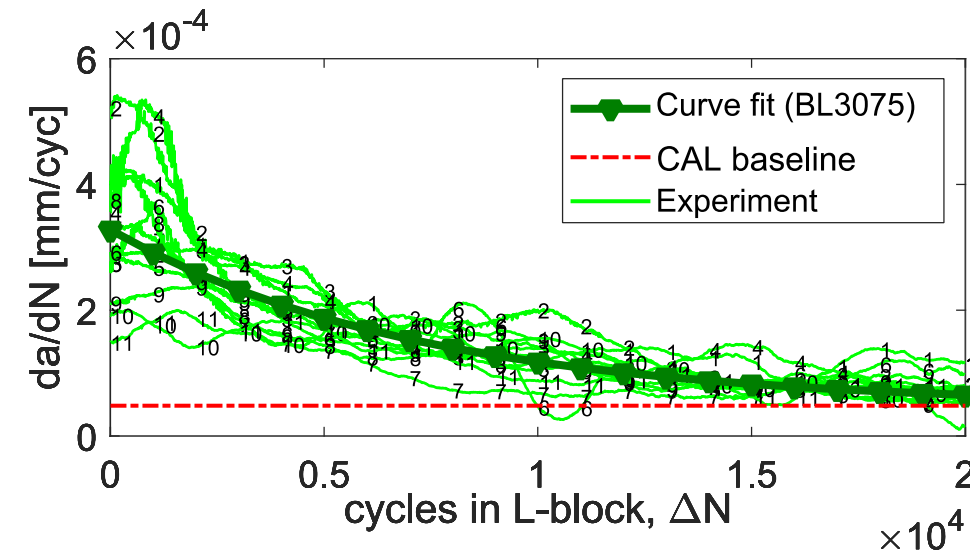
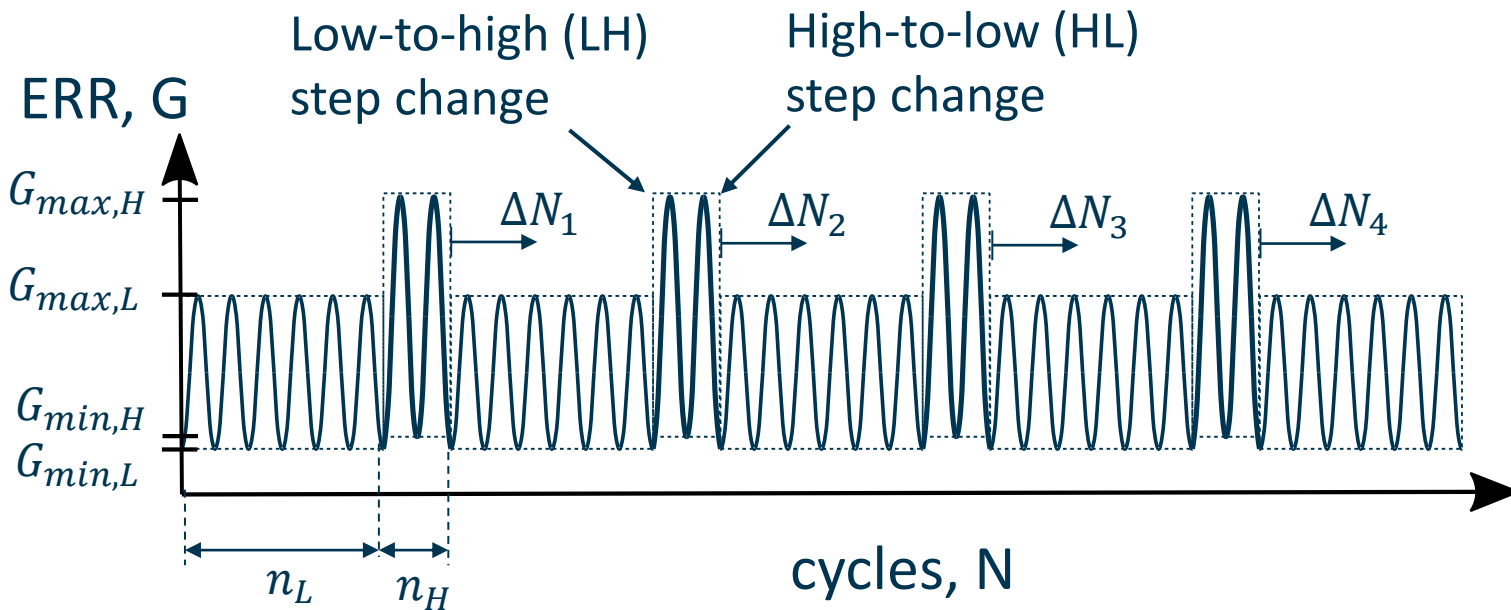


- The same setup is convenient to analyze **transient crack growth** (see example)
- Transient phenomena have been identified (Jensen et al., 2021) and proved significant
- **Current focus:** Find CGR functions to describe the transient phenomena



Characterize cyclic transient crack growth

- Apply **two-level block loading** to DCB specimens in ERR-control
- To characterize the **transient CGR following HL step changes**:
 - Measure CGR following every HL step change and generate $(\Delta N_j, da/dN)$ -curves
 - Superimpose results
 - Generate curve fit
- Transient CGR is well-described by an **exponential decay function**



Transient CGR functions

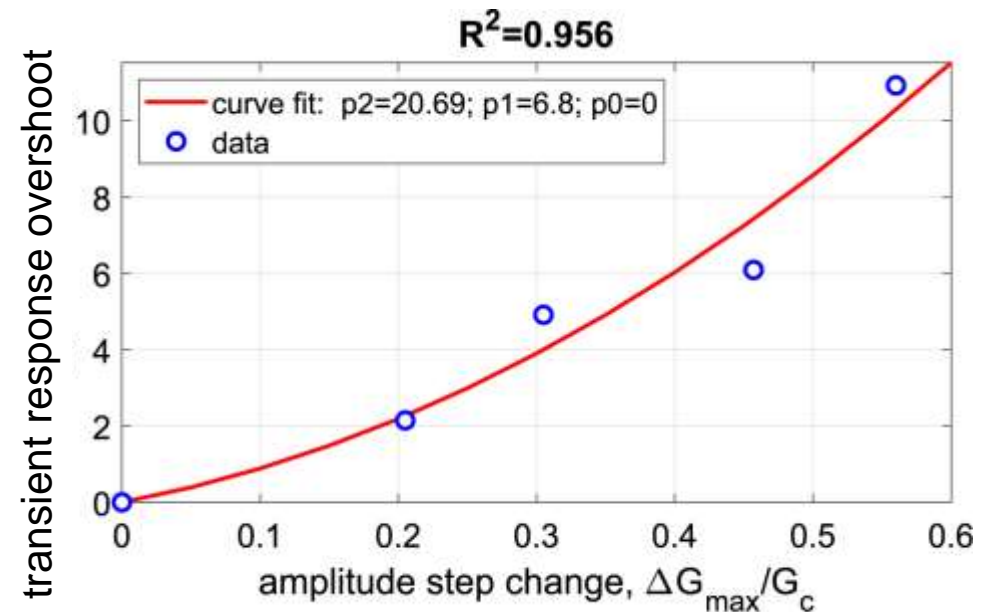
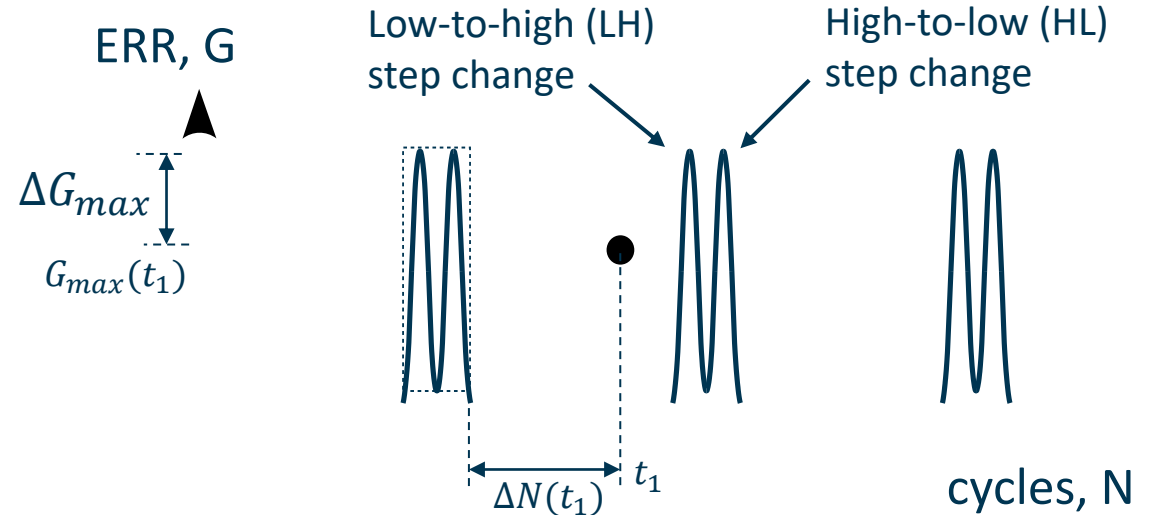
- Investigate **how the transient responses vary with** fatigue load parameters, for example ΔG_{max}
- The transient term in the CGR model will be described by an **exponential decay function, F_{tr}** :

$$\frac{da}{dN_{tr}} = F_{tr} \left(\underbrace{G_{max}}_{\text{Instantaneous}}, \underbrace{\Delta N, \Delta G_{max}}_{\text{Load history}} \right)$$

In:

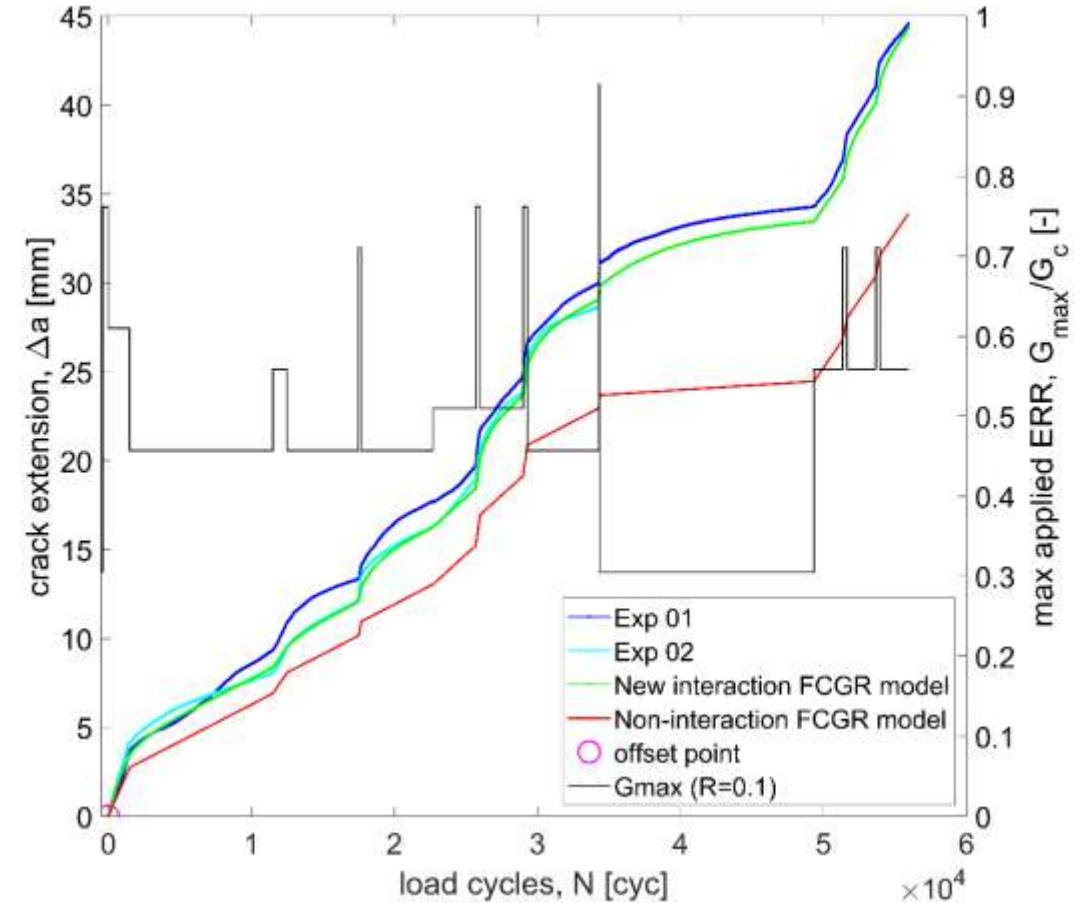
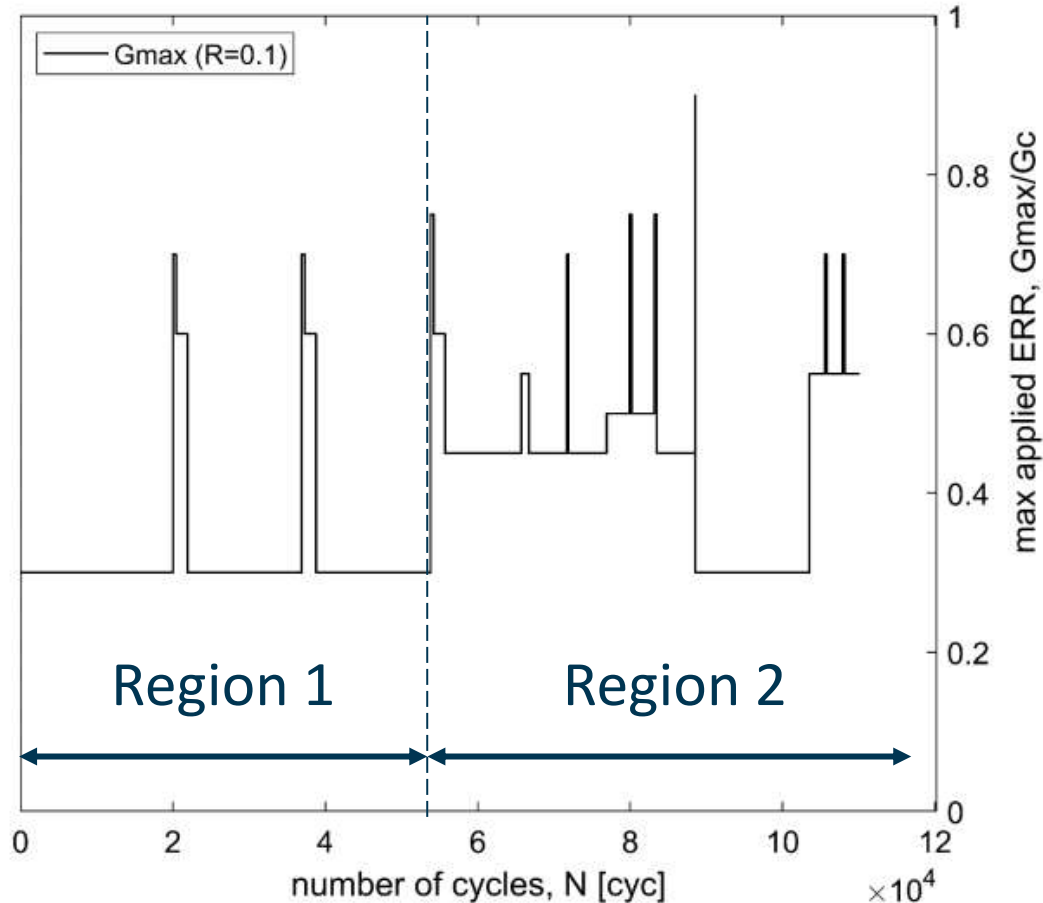
$$\frac{da}{dN} = \frac{da}{dN_{SS}} + \frac{da}{dN_{tr}}$$

- Note: The model only includes transient responses following **HL step changes**. Transient effects due to **LH step changes** are neglected.



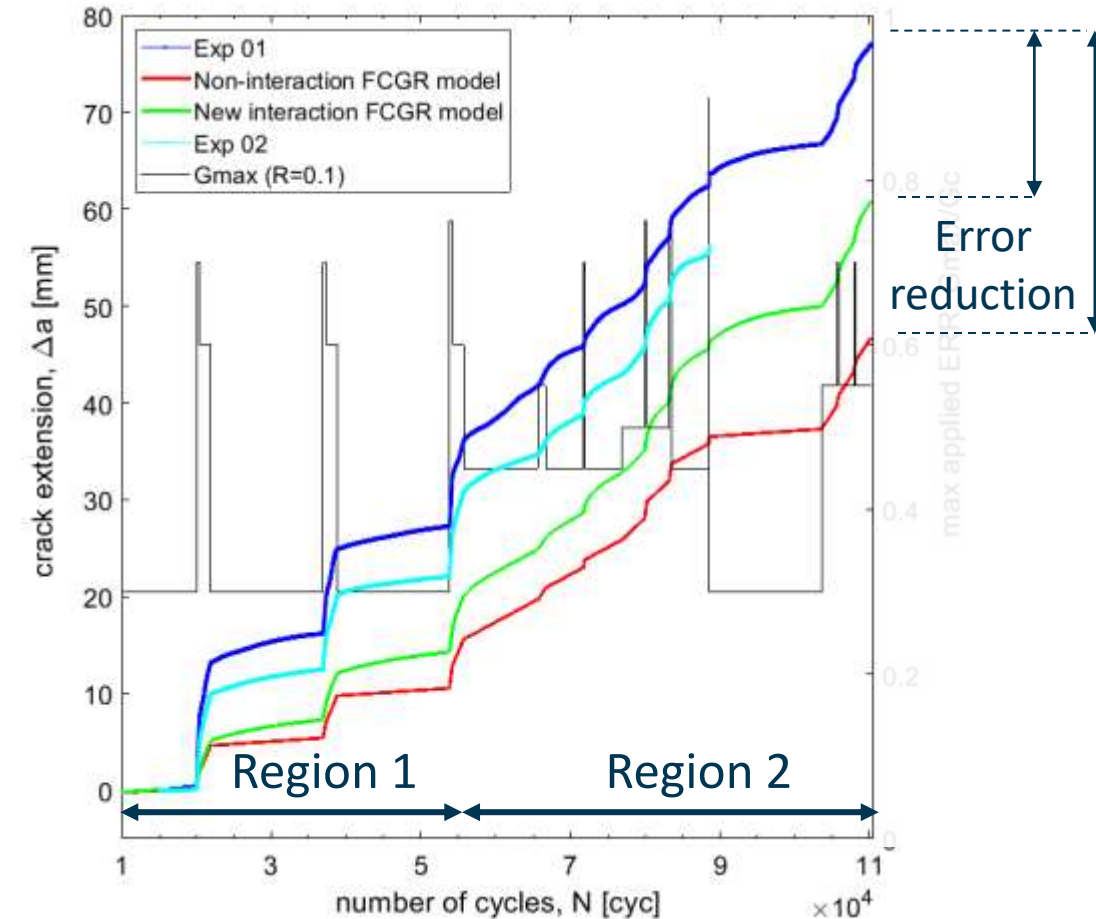
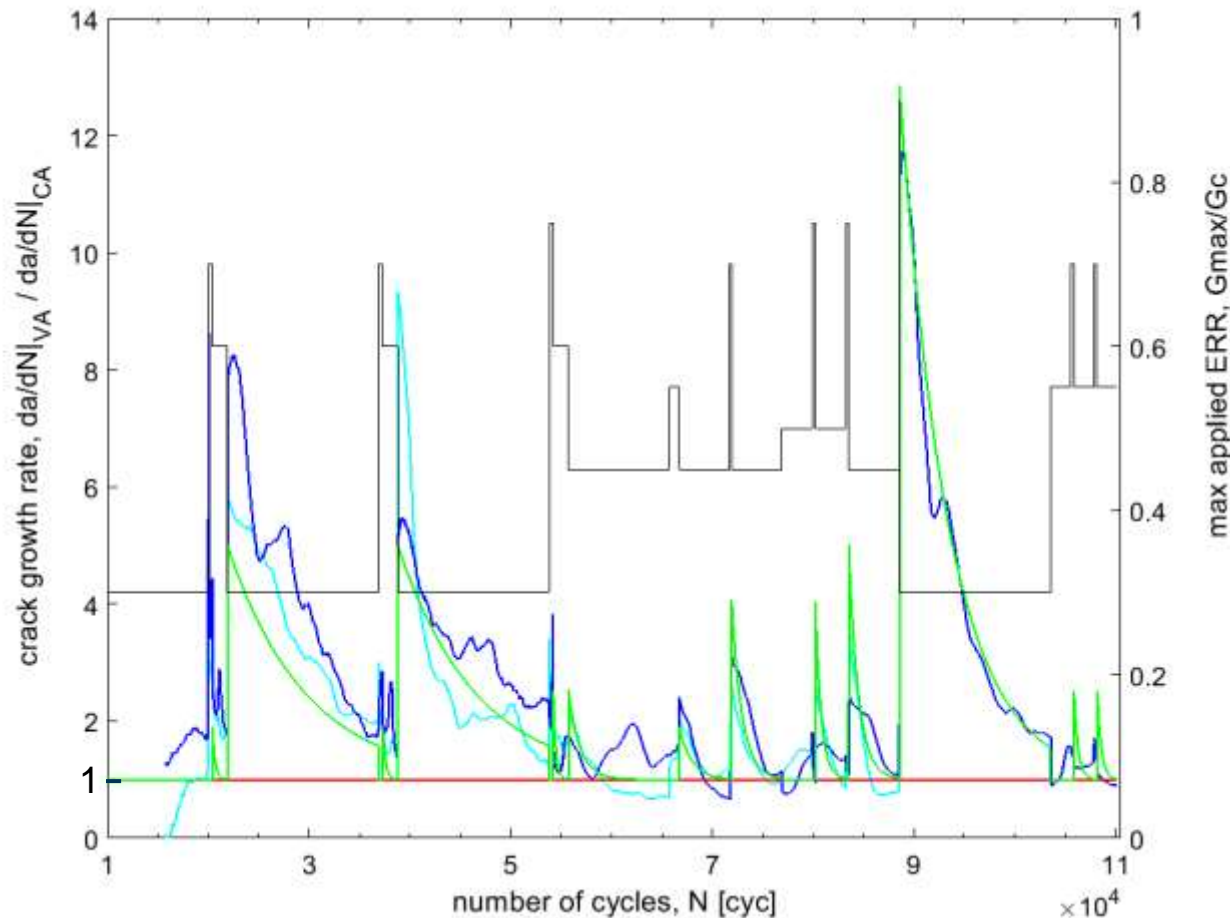
Multi-level block loading benchmark: Region 2

- How will the model perform in the multi-level block loading test? It depends...
- Good results for **Region 2**: Total crack extension and transient phenomenological behaviors

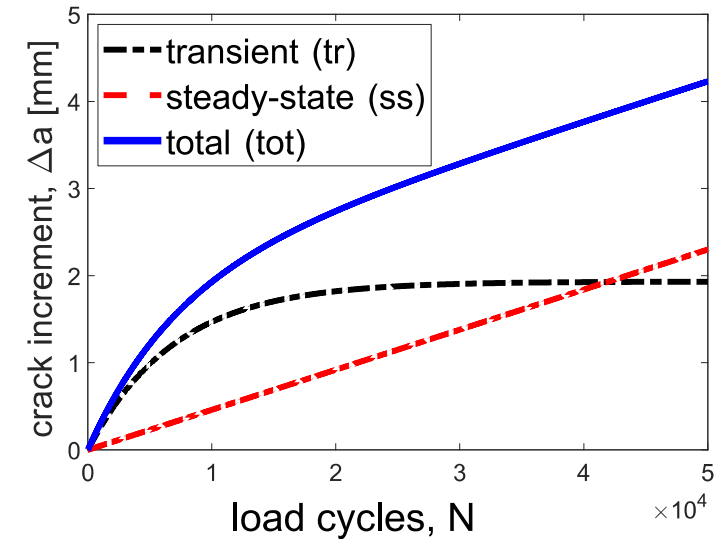
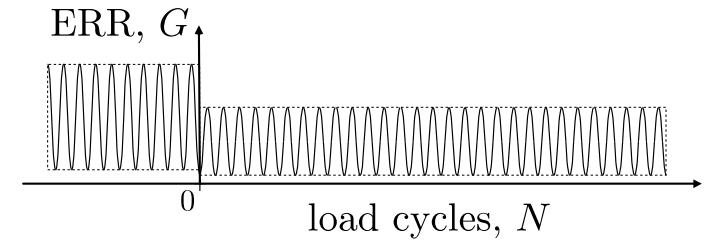


Multi-level block loading benchmark: Full

- An error remains – partly due to the neglected transient effects following **LH step changes**
- The experimental CGR is clearly different from the non-interaction model
- The new CGR model **captures exponential decay-type responses** at HL step changes

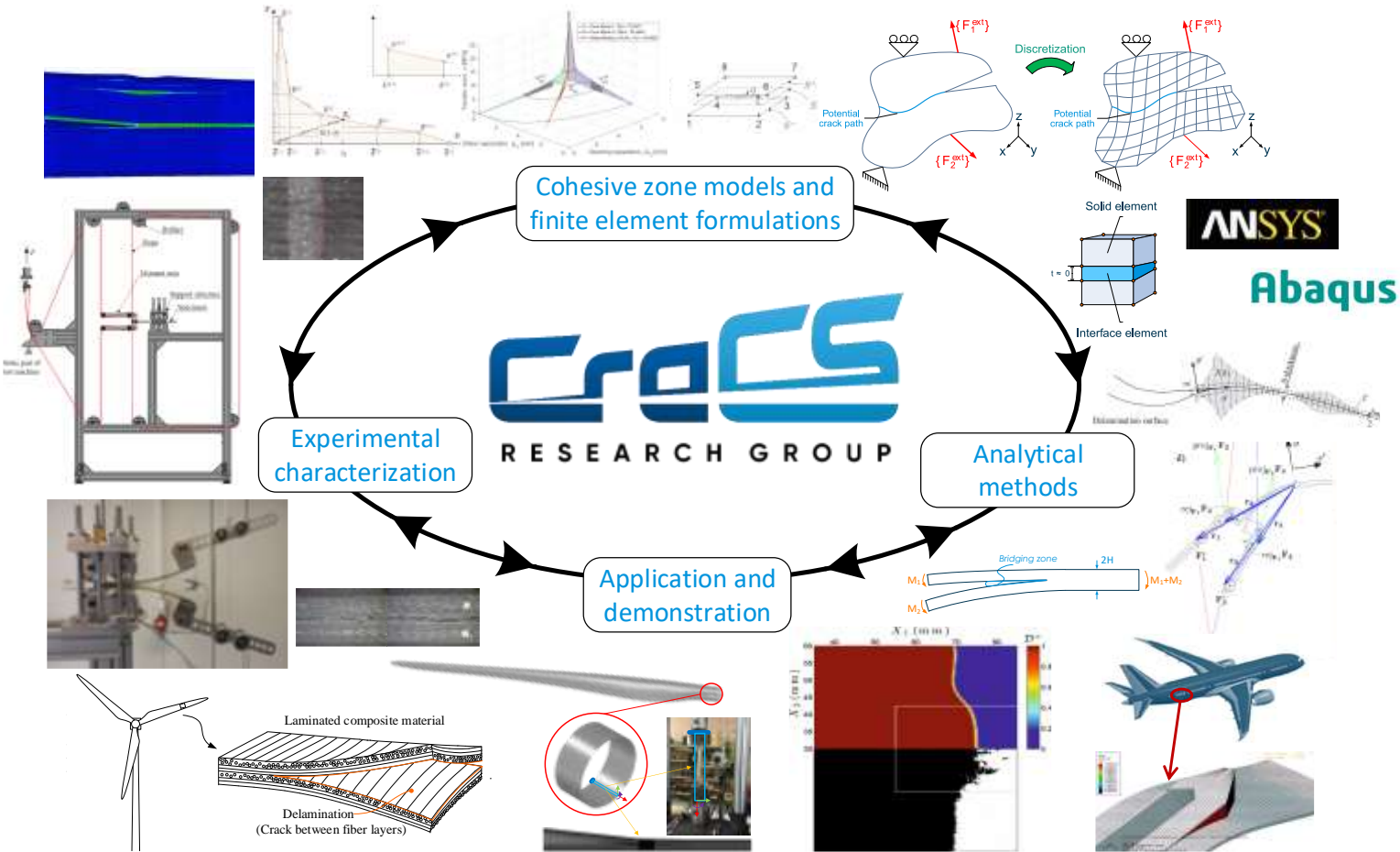


- The CGR following amplitude step changes can be decomposed into a **steady-state** and **transient** response
- A method to characterize steady-state and transient CGR functions is proposed using **ERR-controlled DCB tests**
- A new **CGR model with load history** effects is formulated
- The model can predict delamination in a significant portion of a **new multi-level block loading benchmark test**

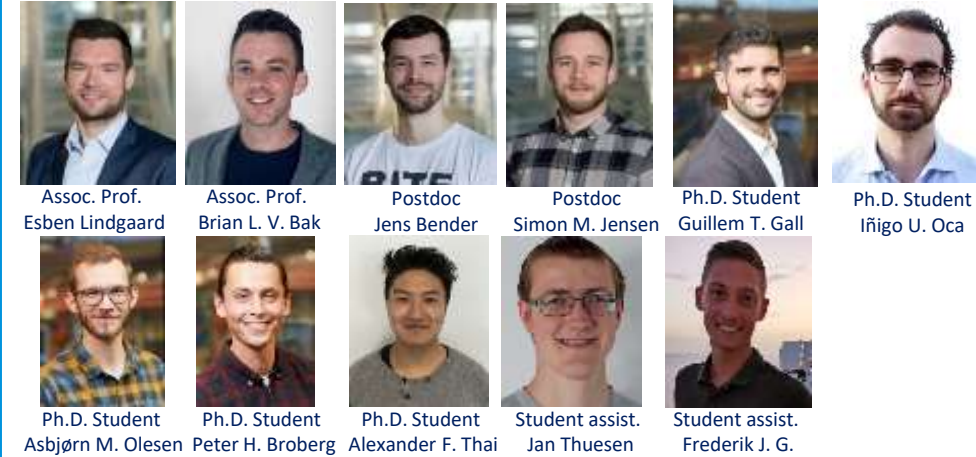


$$\frac{da}{dN} = \frac{da}{dN_{ss}} + \frac{da}{dN_{tr}}$$

THANK YOU FOR YOUR ATTENTION



The CraCS team:



Project partners:



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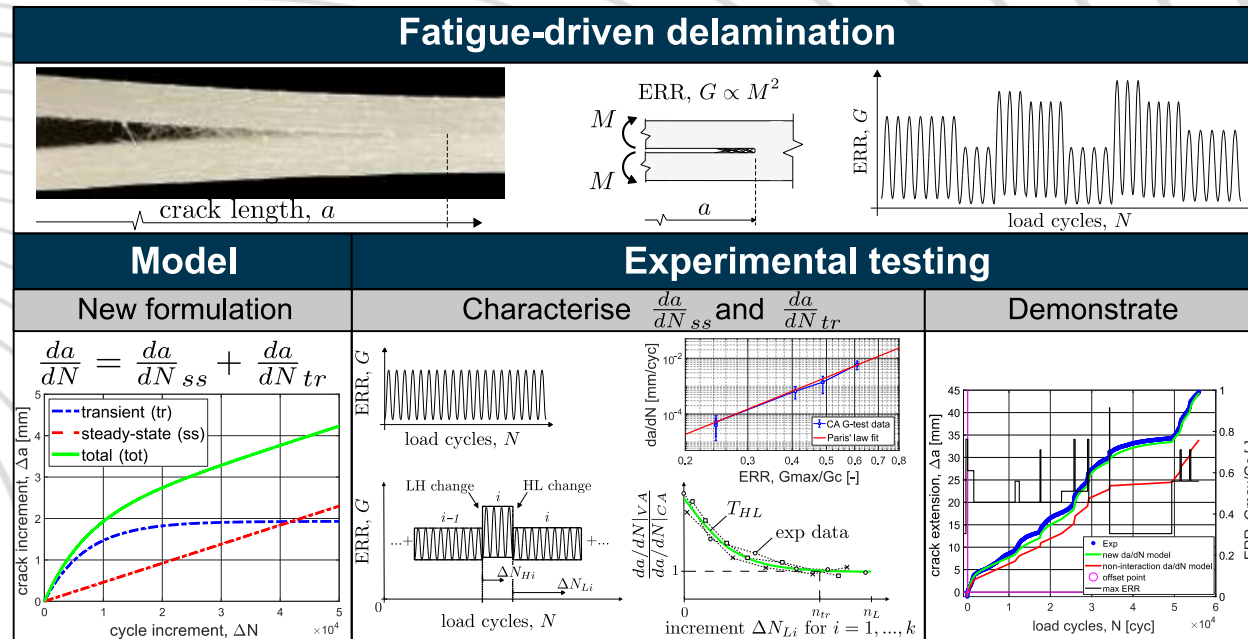
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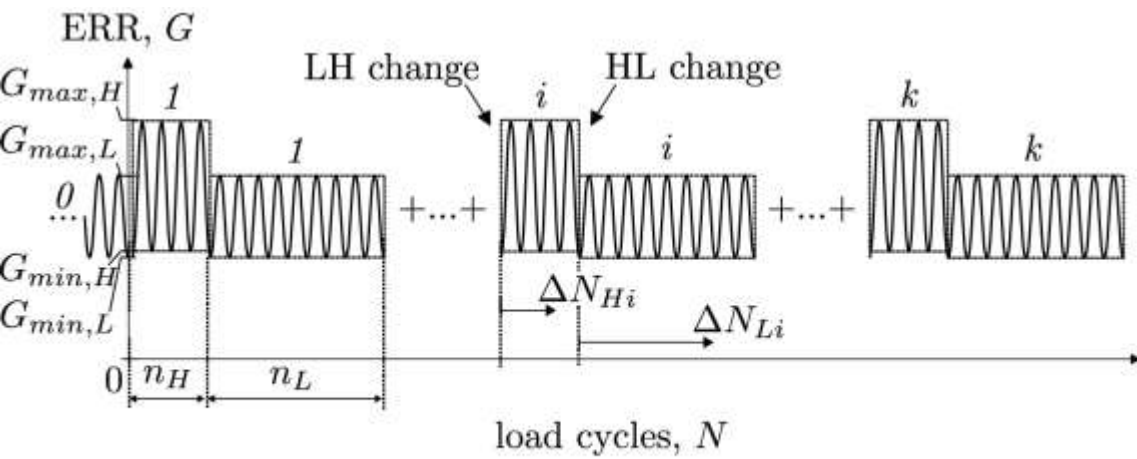
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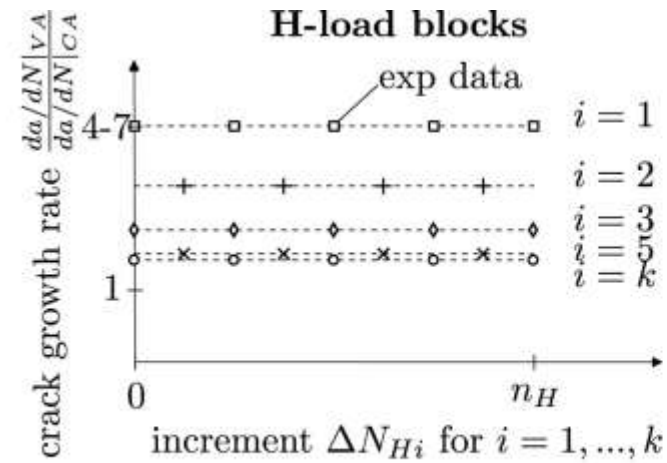


BONUS SLIDES

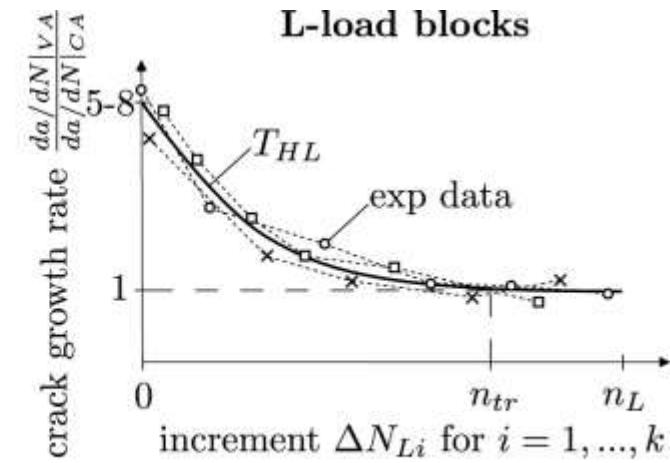




(a)

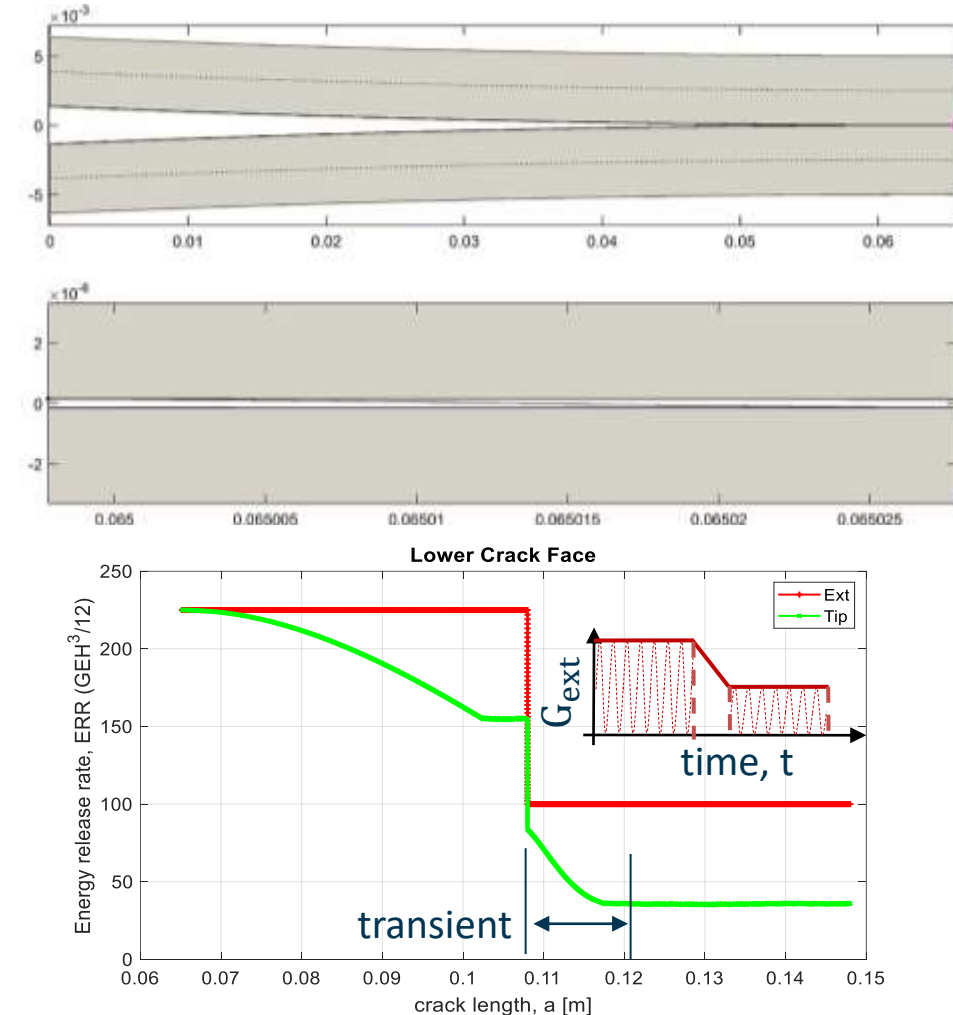


(b)



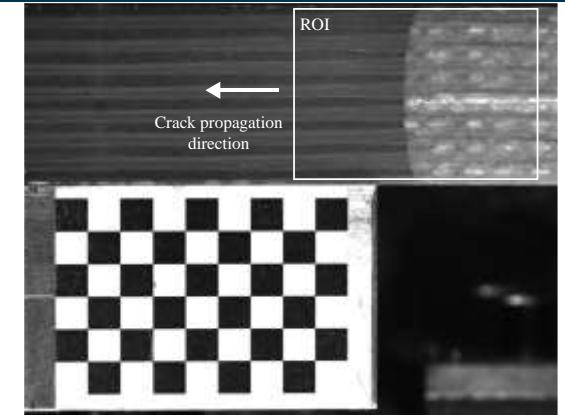
(c)

- A phenomenological model: **Transient** responses are **not derived from the actual physical** processes on meso-/micro-scale
- The model ignores the underlying mechanisms and **concentrate on the gross macroscopic crack tip** propagation using empirical relations, $f_{tr}(ERR)$
- **Physical-based models** of governing mechanisms in the FPZ and their interaction are necessary
- How are the crack tip shielding effect of bridging fibers other **underlying mechanisms affected by VA loading?**

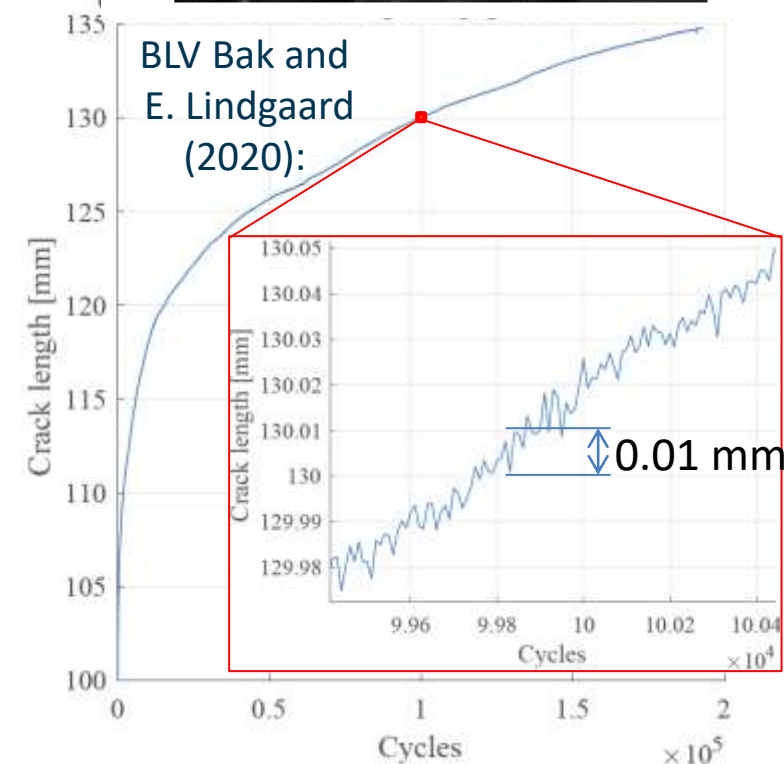
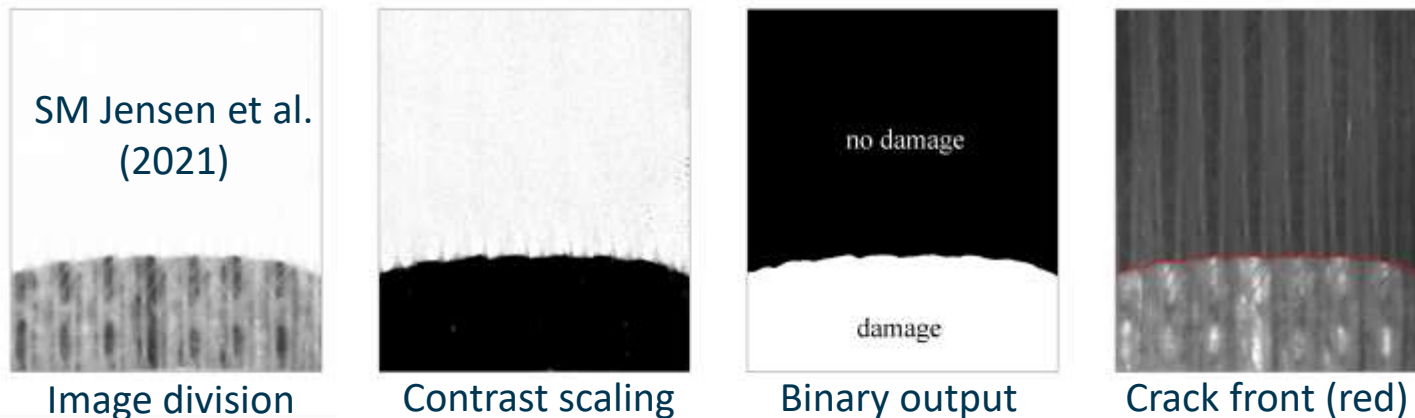


Jensen SM, Bak BLV, Lindgaard E & Renart J (2021) *Micromechanisms of load history effects in fatigue-driven delamination growth*, 8th ECCOMAS thematic conference on the mechanical response of composites 2021, Gothenburg, Sweden.

- Crack length measurements: A camera records the top surface of the DCB specimen (FOV).
- A fully automated and continuous process.
- Low noise and high resolution in crack front identification.
- Important when detecting small crack increments due to load interactions.



Digital-image based technique and image processing operations:



- A highly capable test setup for detecting small Δa due to the isolated effect of load interactions is a prerequisite.
- Highlight two features which are especially important here:
 - G-controlled cyclic testing using the pure moment loaded DCB test configuration.
 - Automated digital image-based technique for tracking of the delamination front.

