¹ Unsymmetrical stacking sequences as a novel approach to tailor ² damage resistance under out-of-plane impact loading

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5 Abstract

In current composite design, stacking sequence symmetry around the laminate mid-6 plane is an unarguable constraint to avoid warpage during manufacturing. However, 7 several load cases induce unevenly distributed stresses through the laminate thickness, 8 such that symmetric laminates may not be the optimal solution. In this paper, we 9 explore the damage resistance to out-of-plane low velocity impact loading of an unsym-10 metrical laminate with zero extension-bending coupling matrix ([B]), thereby assuring 11 no undesired coupling deformations during mechanical or thermal loads. Using impact 12 and quasi-static indentation tests, C-scan inspection and numerical modelling, we com-13 pare the damage pattern between an unsymmetrical laminate with ply clustering at the 14 impacted face and a laminate with ply clustering at the non-impacted face (produced by 15 flipping the former laminate upside down). The laminate with clusters at the impacted 16 side exhibits better damage resistance for lower impact energies. More importantly, the 17 location of the damage events obeys the predictions assumed when the laminate was de-18 signed, demonstrating the room for improvement by tailoring unsymmetrical laminates 19 to particular load cases. 20

- ²¹ Keywords: B. Impact behaviour, B. Delamination, C. Damage mechanics, C. Finite
- ²² element analysis (FEA), Unsymmetrical laminates

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23 1. Introduction

Impact loading and the threat it poses to composite structures is a matter of concern 24 for aircraft engineers and researchers. The severity of the impact induced damage 25 and its propagation during in-flight loads is the key research question to be answered 26 as impact damage can reduce the residual strength of a structure by up to 60% [1]. 27 In an effort to improve damage resistance, researchers have gone one step further in 28 laminate design and have proposed non-conventional laminates using dispersed angles 29 [2-4], varying mismatch angle at interfaces [4; 5] or selective ply clustering [6]. Despite 30 the novelty in laminate designing, symmetry around the mid plane of the laminate 31 remains an unquestioned constraint, mainly to avoid warpage during manufacturing 32 and coupling responses under loading [7]. 33

Impact loading is a complex loading case because of the interaction of different 34 damage mechanisms, mainly in terms of matrix cracks and delamination, followed by 35 fibre failure at higher impact energies. The damage scenario is unsymmetrical in the 36 through-the-thickness direction [8; 9]: high contact compressive stresses cause matrix 37 cracks by shear at the vicinity of the impactor (impacted face of the laminate), whereas 38 tensile stresses cause transverse matrix cracking at the non-impacted face of the lam-39 inate. These cracks grow into the interfaces and initiate delamination oriented in the 40 direction of the lower plies [8]. Acknowledging that the impacted and non-impacted 41 laminate sides experience different damage mechanisms during impact, the constraint 42 of laminate symmetry needs to be challenged. 43

Recently, quasi-static indentation (QSI) tests are considered as an alternative to the low velocity impact tests, due to the similarity in the loading responses and the damage characteristics [10–12]. In LVI loading, the impact contact time is long enough to allow the impact waves to get reflected multiple times from the specimen boundaries and hence the resulting impact response is considered purely static loading [13–15].

⁴⁹ In this paper, we propose an unsymmetrical laminate with ply clustering at the ⁵⁰ impacted face of the laminate. As reported in [13], a clustered ply block induces high

interlaminar shear stresses thereby triggering delamination at the corresponding ply 51 interface. Here we attempt to use localized ply clusters in the laminate to foster de-52 lamination at pre-determined regions. Thanks to the unsymmetrical design, the same 53 laminate, when flipped upside down, produces another stacking sequence with ply clus-54 tering at the non-impacted face. Low velocity impact (LVI) and quasi-static indentation 55 responses of these two unsymmetrical laminates are studied in order to shed light on 56 how the initiation and propagation of the delaminations differ when imposed at different 57 locations. Further, numerical results from an in-house finite element model featuring 58 inter and intralaminar damage are compared with the experimental results, followed 59 by an in-depth energy dissipation analysis for each ply and interface of both laminates. 60 To the authors' knowledge, this is the first report on an experimental impact study on 61 an unsymmetrical laminate. 62

63 2. Unsymmetrical laminate design

The unsymmetrical laminate was obtained by means of an optimization algorithm (genetic algorithm embedded in the MATLAB optimization toolbox [16]). The objective function was a minimum summation of the terms of the B matrix, with the intention of finding solutions with a null B matrix. A null B matrix assures that there is no extension-bending coupling response [17; 18] and as a result there will be no undesired deformation couplings such as warpage during manufacturing.

In addition to the objective function, the following constraints were also imposed: 70 i) the laminate had to be in-plane quasi-isotropic and balanced with 24 plies; ii) as ply 71 clustering induces delamination at the interfaces of the blocked plies [13; 19], four clus-72 ters (one cluster for each orientation, 0° , $\pm 45^{\circ}$ and 90°) were imposed at the impacted 73 side of the unsymmetrical laminate to trigger delamination at these locations; it was 74 also made sure that not more than three plies of the same orientation were stacked 75 together; iii) the surface ply was fixed to be either 45° or -45° in order to tackle the 76 shear loads [2]; and iv) a constant mismatch angle of 45° was used at the interfaces, 77 thereby avoiding the effect of varied mismatch angled interfaces [4; 5]. 78

The solution, with a zero B matrix was: $[-45_2/90_2/45_2/0_3/45/90/-45/0/45/90/-$ 80 45/0/45/90/-45/0/45/90/-45].

3. Methodology

82 3.1. Experimental

The unsymmetrical panel was manufactured using Hexcel[®] IM7/8552 uni-directional prepreg tapes and was cured in an autoclave. Despite being unsymmetrical, the panel had zero warpage after curing; as expected from the design study of the stacking sequence.

Impact specimens of standard 150 x 100 mm dimensions were cut out of the panel 87 with 0° plies aligned in the longer direction. The 24-ply laminate had a cured thickness 88 of 4.36 mm and a ply thickness of 0.182 mm. The specimens cut out were flipped upside 89 down in order to obtain specimens with the same ply clustering at the non-impacted 90 side. The laminate with ply clustering at the impacted side is hereafter called LPCI, 91 and the laminate with ply clustering at the non-impacted side as LPCN (Fig. 1). It is 92 to be noted that flipping a laminate upside down only interchanges the -45° plies with 93 45° plies, thus both laminates have the same in-plane stiffness in all directions and the 94 same bending stiffnesses in the 0° and 90° directions. 95

As in [13; 20], impact tests were performed on 150 x 100 mm specimens in accordance with the ASTM D7136/D7136M-15 standards [21] using a CEAST Fractovis Plus instrumented drop-weight tower. The impactor featured a 16 mm in diameter hemispherical tip and the impactor mass was adjusted to 5 kg for the entire study. As the study aims to analyse the low velocity impact response (energy levels that create lesser damage than the barely visible impact damage (BVID) threshold) of the laminates, two LVI energies, 12 J and 18 J, were explored.

QSI tests were performed using an MTS INSIGHT[®] 50 testing machine with a 50 kN load cell, replicating the same boundary conditions as the impact test. Specimens were placed on a base support with an open window of 125 x 75 mm and clamped at the edges using four rubber pads. Displacement controlled indentation was performed ¹⁰⁷ on the specimens at a rate of 1 mm/min using the same indenter configuration as for ¹⁰⁸ impact loading. Further details of the test setup are provided in [22].

QSI loading was interrupted for C-scan damage inspection followed by further inden-109 tation to the next indenter displacement level, thereby the same specimen was subjected 110 to more than one indentation. A total of 8 indenter displacements (from d = 1.17 mm 111 to 5.4 mm) were investigated, thus obtaining the complete damage evolution starting 112 from the initiation of matrix cracks to complete delamination propagation. The in-113 denter displacements were defined on the go: the indentation was stopped when a load 114 drop or a change in stiffness of the force-displacement response, or an acoustic emission, 115 was noticed. 116

Pulse-echo mode ultrasonic C-scan inspection was performed on all the QSI specimens after each displacement level and on all the impacted specimens using an OLYM-PUS OMNI MX system employing a 5 MHz piezoelectric probe. As C-scan inspection has the drawback of larger delaminations masking the underlying ones, C-scan was performed from both sides of the specimens, and the results presented are the inspections providing the most information.

123 3.2. Numerical modelling

User-defined constitutive models from Maimí et al. [23; 24] were used to simulate 124 the onset and propagation of intralaminar damage. Apart from the main highlights 125 such as crack closure effects, incorporating in-situ effects [25; 26], and the inclusion 126 of crack band model formulation, the complete description can be found in [27]. The 127 model was implemented as an Abaqus/Explicit VUMAT user-written sub-routine. The 128 interlaminar damage was modelled using the ABAQUS Explicit in-built surface based 129 cohesive behaviour [28], where a contact based interaction is used to model the traction 130 between the contact surfaces to simulate delamination. The delamination initiation 131 is governed by a quadratic stress-based criterion implemented in ABAQUS, whereas 132 delamination evolution is characterised by the mixed mode energy-based propagation 133 criteria proposed by Benzeggagh and Kenane [29]. Formulations of the initiation and 134

¹³⁵ propagation criteria are not detailed here but can be found in the work of Tan et al.¹³⁶ [30].

This study follows a novel FE modelling approach from González et al. [27]. In-137 terested readers are referred to their work for a more detailed description. Each ply is 138 modelled using a conventional shell element which is sandwiched by surface elements 139 on the top and bottom faces of the ply. The surface elements are tied to the shell ele-140 ments with rigid tie connectors, thereby transferring the kinematics from the shells to 141 the surface elements. Delamination between two plies is modelled by assigning cohesive 142 surface-based interaction between the bottom face of the surface elements of the top 143 ply and the top face of the surface elements of the bottom ply, as seen in Fig. 2 for an 144 illustrative two plies model. 145

Clustered plies were modelled as a single shell element layer, leading to a model 146 consisting of 19 layers. S4R conventional shell elements were used for the plies and 147 SFM3D4R for the surface elements. The mesh was finer under the impactor (a refined 148 window of 75 by 75 mm, referenced from the impact centre, with element size, l =149 0.5 mm) than elsewhere (l = 4 mm). Moreover, the in-situ effect is accounted for by 150 considering the ply thickness and the ply type (outer and embedded). To avoid exces-151 sive element distortion, an element was deleted when the fibre damage variable (d_1) 152 reached 1, whereas the transverse (d_2) and shear damage (d_6) variables were assigned a 153 maximum value of 0.99, and no element deletion was considered. A friction coefficient 154 of $\mu=0.3$ was assumed at the ply interfaces, as this property is not experimentally avail-155 able. Further details about modelling (impactor, rubber clamps, base plate), contact 156 algorithms, cohesive law shapes are explained in detail in [27; 31; 32]. The material 157 data for IM7/8552 was obtained from [33]. 158

159 4. Results

160 4.1. Experimental

The delamination threshold load, F_d , marked by the first clear load drop in the impact curves at 12 J and 18J (Fig. 3), is 30% higher for LPCI than LPCN, thereby

LPCI clearly delays delamination onset compared to LPCN. After the delamination 163 threshold load, a comparatively unstable response associated with intermittent load 164 drops is seen with LPCI over LPCN. Maximum peak load, F_{max} , is approximately the 165 same for both laminates at 12 J, whereas an increase of 12% is observed for LPCN over 166 LPCI at 18 J. The energy dissipation of LPCI is 9% and 22% larger than LPCN for 167 12 J and 18 J, respectively. A compact quantitative overview of the various damage 168 resistance parameters for both laminates and both impact energies is presented using 169 a radar plot in Fig. 4. 170

Fig. 5 identifies the delaminated interfaces as well as the dominant delaminations for 171 both laminates. Dominant delaminations are those which govern the total delamination 172 profile, thereby playing a major role in the damage tolerance of the structure [22; 34]. 173 For LPCN, they appeared at all the interfaces within the clustered block (interfaces 15, 174 16, 17 and 18) and scaled up when moving from 12 J to 18 J. For LPCI, an unsymmetric 175 delamination profile is observed for 12 J, with the dominant delaminations at interfaces 176 within the clustered block at the impacted side (int. 3, 4) as well as just below the 177 clustered block (int. 5, 6, 7). Moving on to the 18 J impact, a rapid growth in the 178 projected delamination size is observed where the dominant delaminations are found 179 outside the cluster block (int. 5, 6, 7), with the 90° oriented delamination (int. 5) almost 180 reaching the impact window boundaries. When both laminates were compared, LPCI 181 displayed a 20% reduced projected delamination area over LPCN for 12 J, whereas at 182 18 J it was 50% larger. 183

Unlike the impact tests, QSI tests interrupted for damage inspection provide infor-184 mation about the whole damage process. Fig. 6 shows the load displacement response 185 of a pristine specimen up to the highest indenter displacement (d=5.4 mm) as well as 186 the other indenter displacements (d_i) , and the associated applied energies (E_a) . The 187 early delamination initiation of LPCN found in the impact test, is observed in the 188 QSI results as well. After the delamination drop, the load deflection response for both 189 LPCN and LPCI from indenter displacement d_3 to d_5 is similar. Beyond this, d_7 to d_8 , 190 LPCI shows a relative reduction in the stiffness followed by an increase. 191

Fig. 7(a) details the complete QSI delamination sequence obtained for both lam-192 inates using interrupted C-scan inspections, thus helping to relate each load drop or 193 stiffness change (Fig. 6) to the corresponding delamination or its propagation. C-scan 194 images of displacement d_1 (just after the first load drop of LPCN and before the load 195 drop of LPCI) evidence the presence of delamination (initiated in the clustered block at 196 the non-impacted side) in LPCN and yet there is no delamination initiation in LPCI. 197 The first load drop is related to a simultaneous occurrence of matrix cracks and delam-198 ination initiation [9; 14]. Displacement d_2 (immediately after the load drop of LPCI) 199 shows delamination initiation in the clustered block at the impacted side of LPCI and 200 delamination extension at the interfaces of the non-impacted side for LPCN. 201

Through displacements d_3 to d_5 , already formed delaminations propagate in both 202 laminates. The LPCI laminate exhibits dominant delamination mainly at the impacted 203 side, whereas in LPCN delaminations at the interfaces of the non-impacted side dom-204 inate. The change in stiffness for LPCI (displacement d_6 in Fig. 6) corresponds to a 205 rapid and unsymmetric growth of delaminations for LPCI within the interfaces 5, 6, 7 206 at the impacted side). At displacement d_7 (associated with the stiffness increase with 207 LPCI), LPCI has its dominant delamination at interface 5 (oriented in 90°) develop 208 into the supported region of the clamping (as seen with 18 J impact results), leading to 209 stress redistribution and thereby an increase in stiffness, while LPCN showed further 210 delamination extension. Ultimately, the last displacement resulted in further scaling 211 up of delamination with LPCN, and delamination growing to the specimen edges for 212 LPCI. 213

Fig. 7(b) depicts a quantitative evolution of the damage resistance parameters for all the indenter displacements. LPCI was seen to be more damage resistant than LPCN, in terms of projected damage area and dent depth, until the displacement of d_6 , at which an overturn in the trend is noted. Comparing the impact results of 12 J with the QSI results for the same applied energy (corresponding to d_5), a good correlation is observed with the maximum peak force and the projected delamination area. Moving to 18 J, the QSI results (corresponding to d_7) slightly over-predict the above two parameters $_{221}$ compared to the impact results (by 8% and 15%, respectively).

222 4.2. Numerical

The numerical predictions of the impact response curves, namely the force-deflection and energy evolution curves (Fig. 8), are in excellent agreement with the experimental results, especially with the energy evolution for both laminates at both impact energies. Fig. 8 also depicts the impactor displacements chosen for the numerical analysis of the energy dissipated through intralaminar and interlaminar damage: marked by circles (A to E) for the force response and by dashed lines for the energy-time curves. This figure also distinguishes the energy dissipated through intralaminar and interlaminar damage.

Moving away from the normal convention of comparing only the projected delam-230 ination contour or the area, we present a 'virtual C-scan', where along with the de-231 lamination profile and area, each delaminated interface is identified and presented as 232 in a C-scan. Fig 9 shows the good agreement between the virtual and experimental 233 C-scan, highlighting the potential of the numerical tools used. With LPCN laminates, 234 the dominating delaminations and their extension is almost replicated in the prediction, 235 although the projected damage area is slightly under-predicted by an average of 8%. 236 For LPCI, dominant delaminated interfaces are correctly predicted, while the unsym-237 metric delamination extension for 12 J and the rapid growth of the close-to-mid-plane 238 delaminations for 18 J are not, thus the projected damage area is underpredicted. 239

Fig. 10 illustrates the two laminates along with the amount of energy dissipated for 240 each ply and each interface for both laminates. The figure quantitatively compares the 241 inter- (delamination) and intra- (matrix cracks and fibre failure) laminar energy dissi-242 pated for all the plies and interfaces between LPCN and LPCI for 12 J. Note that the 243 different colour codes in the figure represent the energy dissipated within the different 244 displacement steps (A to E, as shown in Fig. 8) considered in the study. The figure 245 also compares (at the bottom) the total energy dissipated (inter- and intralaminar) by 246 the two laminates within the selected displacement steps. 247

²⁴⁸ With LPCN, as demonstrated by the experiment, the last four interfaces (15, 16,

²⁴⁹ 17 and 18) dissipate the larger amount of energy through delaminations, whereas with ²⁵⁰ LPCI the interfaces 3, 4 (within the cluster), 5, 6, and 14 dominate. The total energy ²⁵¹ dissipated by the dominant delaminations of LPCN over its other delaminated interfaces ²⁵² is much higher (int. 15, 16, 17 and 18 account for 30% of the total interlaminar energy ²⁵³ dissipated) than for LPCI. In the case of intralaminar damage, the first four plies of ²⁵⁴ both laminates dissipated most of the energy, with LPCI being comparatively higher ²⁵⁵ than LPCN, due to the clustered plies.

Displacement level A (chosen to be before the load drop for LPCN and before the 256 stiffness change for LPCI in the numerical curve, as in Fig. 8) reveals no delamination 257 for both laminates. Most of the delamination energy dissipation is observed at the 258 final loading part, between the points C and D. The same occurs with the intralaminar 259 damage, with local fibre failure being seen at the top two plies in the vicinity of the 260 impactor. Fig. 10 compares the energy dissipation at the laminate level: the average 261 energy dissipated through delaminations is approximately five times higher than that 262 of the intralaminar damage, signifying the dominance of energy disspation through 263 delamination within the energy levels explored. Comparing LPCI and LPCN for 12 J, 264 LPCI dissipates 18% more energy through intralaminar damage, and 17% less through 265 interlaminar damage. 266

²⁶⁷ 5. Discussion

The experimental results revealed the different damage onset and evolution of the 268 two laminates analysed. Delamination initiates earlier in the laminate with clustered 269 plies at the non-impacted side (LPCN), which is related to the transverse cracks in the 270 plies (at non-impacted side) induced by in-plane tensile loads from laminate bending. 271 These cracks grow into the next available interface to initiate delamination. Clustered 272 plies introduce high bending stiffness mismatch [19], leading to high interlaminar shear 273 stresses at the adjacent interfaces. This triggers delamination and makes clustered 274 plies a weak zone for delamination onset. Additionally, the reduced in-situ effect of the 275 clustered plies favours transverse cracking when compared to the non-clustered plies 276

[33]. When the transverse crack reaches the adjacent interface, the large energy release 277 rate available acts as a catalyst for delamination. Substantial difference in damage 278 mechanisms was observed when the clustered plies are on the impacted side (LPCI). 279 Impact loading introduces high local out-of-plane compressive stresses at the vicinity 280 of the impactor, which counteract the interlaminar shear stresses and lead to increased 281 interlaminar friction [35]. This can be indirectly ascribed to the increase in mode 282 II fracture toughness at regions close to the impactor, as reported in [36; 37]. This 283 constrains the delamination propagation, as observed in the first two interfaces within 284 the clustered block of LPCI (see Fig. 5). 285

We also observed that the position of the larger delaminations varies from one 286 laminate to the other. The idea of imposing delaminations at the non-impacted side 287 in LPCN by tailoring clustered plies has paid off, with the dominant delaminations 288 appearing at the interfaces within the clustered block (int. 15, 16, 17 and 18 in Fig. 289 5). In the case of LPCI, with the suppressed delaminations at the interfaces of the 290 impacted side, the dominant delaminations were seen outside the cluster, due to the 291 high interlaminar shear stresses at the laminate mid-plane. These high stresses trigger 292 transverse shear cracks in the 45° and -45° plies (associated with the interfaces 5, 6 293 and 7 in Fig. 5) promoting delamination oriented in the 90° ply (which is placed in 294 between the 45° and -45° plies as in Fig. 1). Finally, in terms of impact resistance, 295 LPCI performed better at 12 J impact and earlier stages of indenter displacements (up 296 to d_6). At higher energy levels, the rapid growth of close to mid-plane delaminations 297 induced more damage than in LPCN. 298

The numerical study identified the local fibre failure caused by the impactor as the prime reason for the high intralaminar energy dissipation at the top plies (at impacted side) for both laminates. Owing to the cluster effect, LPCI showed higher values of intralaminar energy dissipation over LPCN for the top plies. While the same clustered plies of LPCN dissipated most of the energy through interlaminar damage, LPCI clustered plies dissipated it through intralaminar damage. This difference in behaviour signifies how the location in the laminate varies the damage mode and its evolution. The lack of accuracy of the numerical prediction of LPCI (as in Fig. 8 and Fig. 9), may be attributed to the inability of shell elements to capture the shear matrix cracks from the out-of-plane shear stresses close to the impactor. This could be tackled by incorporating a full three dimensional constitutive behaviour with solid elements [38] followed by a oriented mesh strategy (as demonstrated in [39]), but at the price of a higher computational time.

What is clear from the study, is that damage can be forced to occur at predetermined 312 locations through judicious laminate designing, and thereby tailor the damage resis-313 tance. Unsymmetrical stacking designs can facilitate this task and raise the prospect 314 of an improved impact damage resistance. Current numerical tools provide a detailed 315 physical representation of the damage mechanisms, so they can efficiently support this 316 innovative design task. A continuation of this work will be to compare unsymmet-317 rical laminates with symmetric quasi-isotropic laminates in terms of impact damage 318 resistance and tolerance (Compression After Impact) to better assess the prospects of 319 unsymmetrical laminates. 320

321 6. Conclusion

For the first time, unsymmetrical stacking sequences have been explored in an exper-322 imental low velocity impact framework. We designed an unsymmetrical laminate (with 323 zero extension-bending coupling, and therefore warp-free) with tailored ply clustering 324 at the impacted side, and flipped it upside down to yield a laminate with ply clustering 325 at the non-impacted side. Both these laminates were tested under low velocity impact 326 and quasi-static indentation loading to study their out-of-plane damage resistance. The 327 experimental and numerical results revealed that clustering at the impacted side delayed 328 the threshold load for delamination by 30% and reduced the projected delamination 329 area by 20% for low impact energies. This improvement derived from a higher energy 330 dissipation through intralaminar damage instead of delamination, the most important 331 damage mechanism for the laminate with clusters at the non-impacted side. Damage 332 patterns from both laminates were compared and, importantly, the dominant delamina-333

tions were observed at the locations predicted during the laminate design. This paper highlights the opportunity to move away from conventional symmetrical laminate design, thereby giving laminate designers the freedom to tailor the stacking sequence according to the expected stress states of given load cases.

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16

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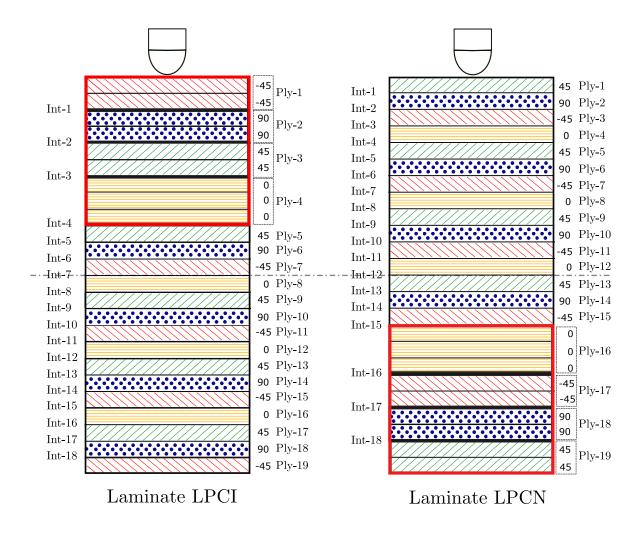


Figure 1: Unsymmetrical laminate LPCI with ply clustering at the impacted side (left) and laminate LPCN with ply clustering at the non-impacted side (right), which is produced by flipping the laminate LPCI upside down. Flipping upside down only interchanges the 45s by -45s plies, i.e., it does not alter the in-plane and bending stiffness in the 0° and 90° directions.

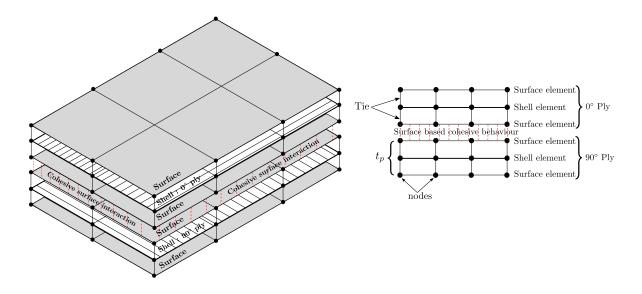


Figure 2: Schematic representation of the modelling strategy, where each ply is modelled using a shell element sandwiched between two surface elements using a tie interaction. Surface based cohesive interaction is assigned between the bottom surface of the top ply and the top surface of the bottom ply. t_p marks the thickness of the modelled ply, and there is no thickness defined between the surface elements.

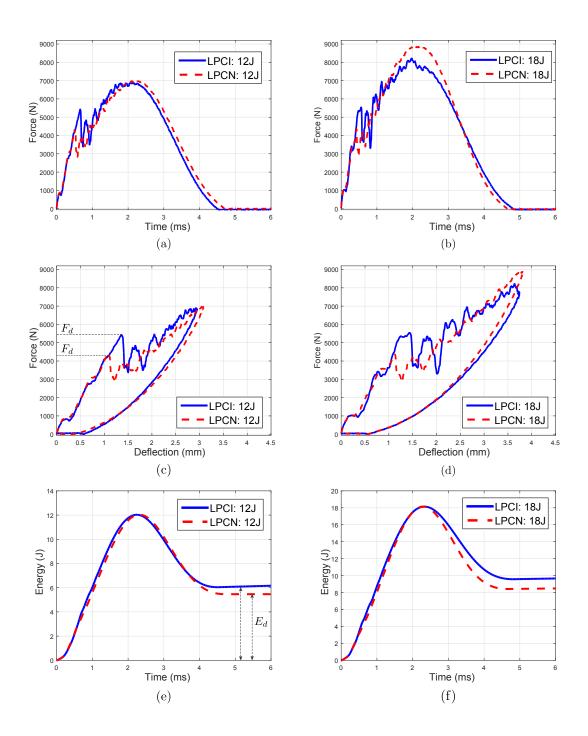


Figure 3: Force-time ((a),(b)), force-deflection ((c),(d)), and energy-time ((e),(f)) response curves for LPCI and LPCN for 12 J and 18 J impact energies.

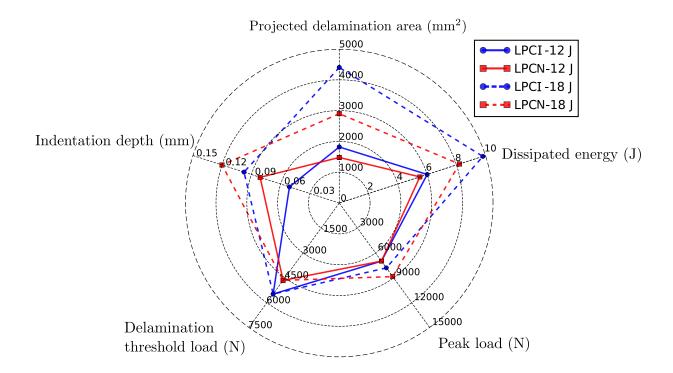


Figure 4: Quantitative overview of impact damage resistance parameters of LPCI and LPCN at both impact energies.

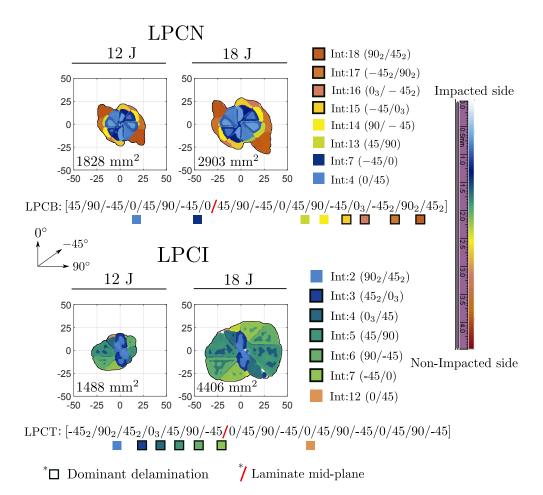


Figure 5: C-scan images of LPCN and LPCI inspected from the impacted face for 12 J and 18 J impact energies. Projected delamination area, identified delaminated interfaces and dominant delaminations are marked (The colour bar helps to identify the location of delamination in the thickness direction, and the axes are provided in millimetres).

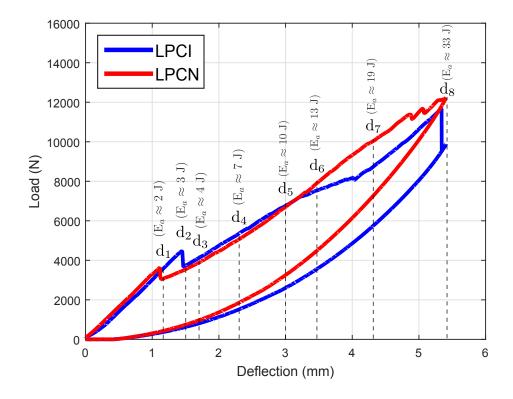
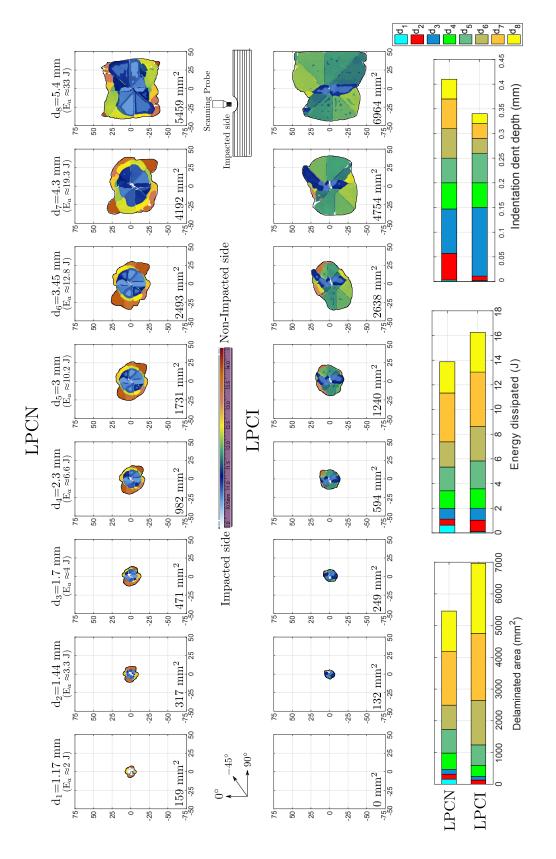
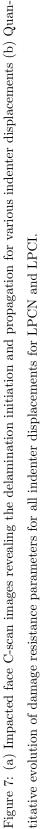


Figure 6: Load-deflection curve for the maximum indenter displacement $d_8 = 5.4$ mm for LPCN and LPCI, also showing the various other indenter displacements used in the study (The respective energy applied, E_a , is also marked for each indenter displacement).





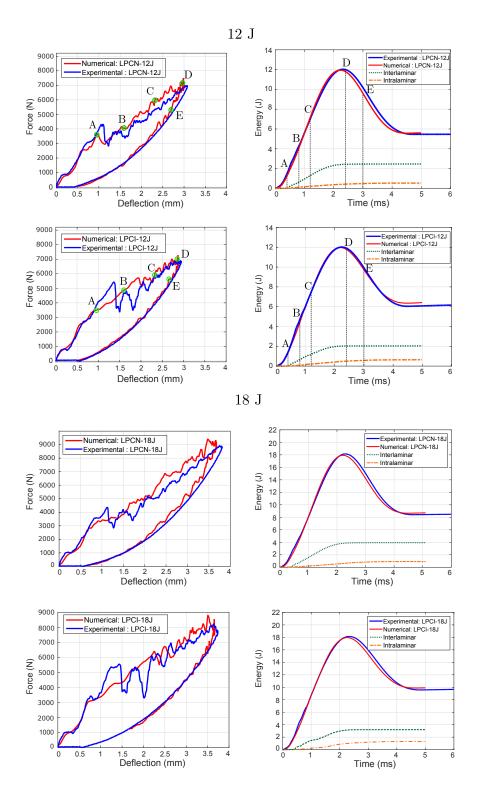


Figure 8: Numerical prediction of the impact response of LPCN and LPCI laminates compared with the experimental data for both 12 J and 18 J. Selected displacements (A to E) for energy dissipation study (in Fig. 10) are also marked for the 12 J energy case.

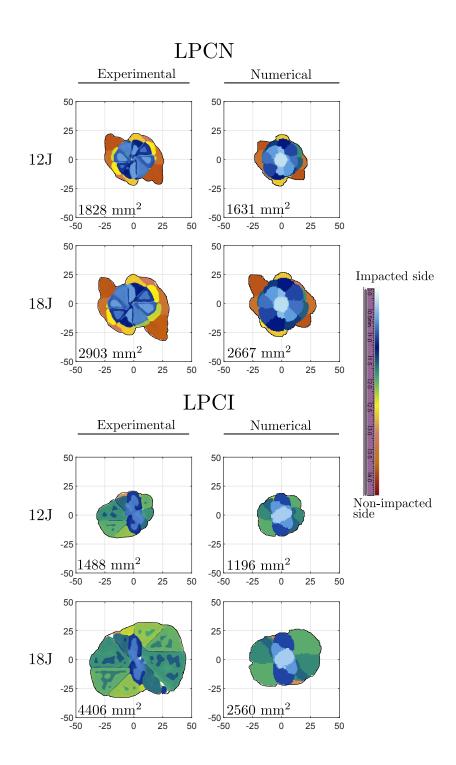


Figure 9: Comparison of the virtual C-scan from numerical study with the C-scan after impact testing for LPCN and LPCI for both 12 J and 18 J. Projected delamination area is provided in the bottom left corner of each box.

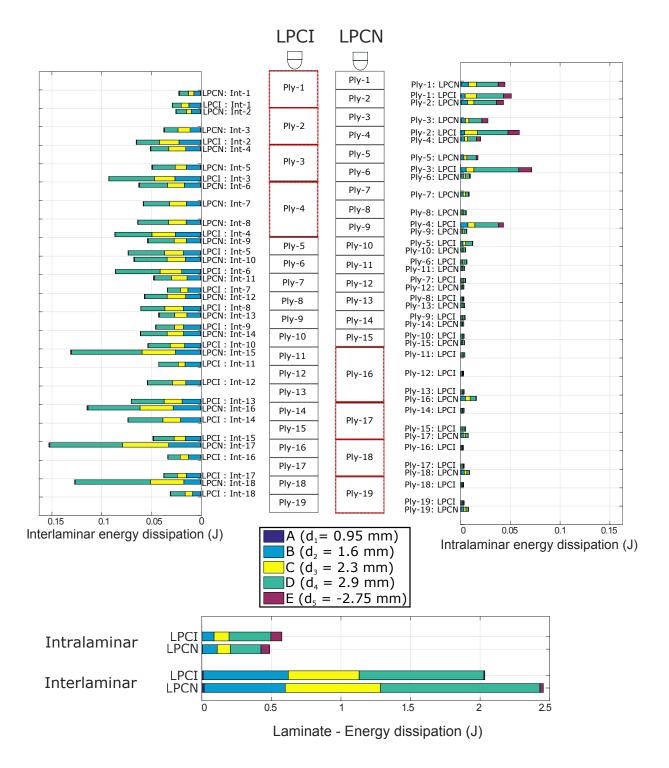


Figure 10: Illustration of the laminates and their plies along with the amount of inter and intralaminar energy dissipated for each ply and interface of both the laminates. Note that the clustered plies are considered as a single ply and hence, for example, interface 1 of LPCI is compared with the interface 2 of LPCN. The different colour codes represent the energy dissipated with the different displacement steps (A to E, as shown in Fig. 8). The total dissipated energies (inter- and intralaminar) by the laminates are also compared at the bottom. 27